## 5.10 all\_incomparable

	DESCRIPTION	LINKS	GRAPH
Origin	Inspired by incomparable rectangle	es.	
Constraint	all_incomparable(VECTORS)		
Synonym	all_incomparables.		
Туре	VECTOR : collection(var-	-dvar)	
Argument	VECTORS : collection(vec	= - VECTOR)	
Restrictions	$\begin{array}{l} \textbf{required(VECTOR, var)} \\  \texttt{VECTOR}  \geq 1 \\ \textbf{required(VECTORS, vec)} \\  \texttt{VECTORS}  \geq 1 \\ \textbf{same_size(VECTORS, vec)} \end{array}$		
Purpose	Enforce for each pair of distinct they are incomparable. Two vectors only, when the components of both SVECTOR1 and SVECTOR2, we ment (for all $i \in [1,  \text{SVECTOR1} ]$ ) nor $i \in [1,  \text{SVECTOR1} ]$ ).	tors VECTOR1 and VEC oth vectors are ordered wither have SVECTOR1	TOR2 are incomparable if and , and respectively denoted by $[i]$ .var $\leq$ SVECTOR2 $[i]$ .var
Example	$\left(\begin{array}{c} \operatorname{vec} - \langle 1, 18 \rangle , \\ \operatorname{vec} - \langle 2, 16 \rangle , \\ \left\langle \begin{array}{c} \operatorname{vec} - \langle 3, 13 \rangle , \\ \operatorname{vec} - \langle 4, 11 \rangle , \\ \operatorname{vec} - \langle 5, 10 \rangle , \end{array} \right\rangle \\ \operatorname{vec} - \langle 6, 9 \rangle , \\ \operatorname{vec} - \langle 7, 7 \rangle \end{array}\right)$		
	The all_incomparable constrain comparable as illustrated by Figure		stinct pairs of vectors are in-
All solutions	Figure 5.21 gives all solutions all_incomparable constraint: $U$ $U_3 \in [0, 6], V_3 \in [2, 5],$ all_incom	$V_1 \in [1,2], V_1 \in [0,$	5], $U_2 \in [3,5], V_2 \in [2,3],$
Typical	$\begin{split}  \texttt{VECTOR}  &> 1 \\  \texttt{VECTORS}  &> 1 \\  \texttt{VECTORS}  &>  \texttt{VECTOR}  \end{split}$		
Symmetry	Items of VECTORS are permutable.		

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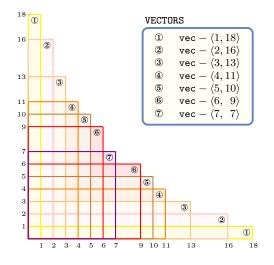


Figure 5.20: Illustrating the incomparability of vectors  $\langle 1, 18 \rangle$ ,  $\langle 2, 16 \rangle$ ,  $\langle 3, 13 \rangle$ ,  $\langle 4, 11 \rangle$ ,  $\langle 5, 10 \rangle$ ,  $\langle 6, 9 \rangle$ ,  $\langle 7, 7 \rangle$ : first to each vector we associate a rectangle whose sizes are the components of the vector; second no matter whether we rotate a rectangle from 90° or not, one rectangle can not be included in another rectangle.

$ \begin{array}{c} \textcircled{1} & (\langle \langle 1, 4 \rangle, \langle 3, 2 \rangle, \langle 0, 5 \rangle \rangle) \\ \textcircled{2} & (\langle \langle 1, 4 \rangle, \langle 3, 3 \rangle, \langle 0, 5 \rangle \rangle) \\ \textcircled{3} & (\langle \langle 1, 5 \rangle, \langle 3, 3 \rangle, \langle 2, 4 \rangle \rangle) \\ \textcircled{4} & (\langle \langle 1, 5 \rangle, \langle 4, 3 \rangle, \langle 4, 2 \rangle \rangle) \\ \textcircled{5} & (\langle \langle 1, 5 \rangle, \langle 4, 2 \rangle, \langle 3, 3 \rangle \rangle) \\ \textcircled{6} & (\langle \langle 2, 4 \rangle, \langle 3, 3 \rangle, \langle 0, 5 \rangle \rangle) \\ \fbox{7} & (\langle \langle 2, 4 \rangle, \langle 3, 3 \rangle, \langle 1, 5 \rangle \rangle) \\ \end{array} $	

Figure 5.21: All solutions corresponding to the non ground example of the all\_incomparable constraint of the **All solutions** slot

Arg. properties	Contractible wrt. VECTORS.
See also	<pre>implies: lex_alldifferent.</pre>
	part of system of constraints: incomparable.
	used in graph description: incomparable.
Keywords	characteristic of a constraint: vector.
	constraint type: system of constraints, decomposition.
	final graph structure: no loop, symmetric.

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**Cond. implications** 

- all\_incomparable(VECTORS) with |VECTOR| = 2 implies k\_disjoint(SETS : VECTORS).
- all\_incomparable(VECTORS) with |VECTOR| = 2 implies twin(PAIRS : VECTORS).

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Arc input(s)	VECTORS
Arc input(s)	VECTORS
Arc generator	$CLIQUE(\neq) \mapsto \texttt{collection}(\texttt{vectors1}, \texttt{vectors2})$
Arc arity	2
Arc constraint(s)	<pre>incomparable(vectors1.vec, vectors2.vec)</pre>
Graph property(ies)	$\mathbf{NARC} =  VECTORS  *  VECTORS  -  VECTORS $
Graph class	• NO_LOOP • SYMMETRIC

Graph model

The Arc constraint(s) slot uses the incomparable constraint defined in this catalogue.

Parts (A) and (B) of Figure 5.22 respectively show the initial and final graph associated with the **Example** slot. Since we use the **NARC** graph property, the arcs of the final graph are stressed in bold. The previous constraint holds since exactly  $3 \cdot (3 - 1) = 6$  arc constraints hold.

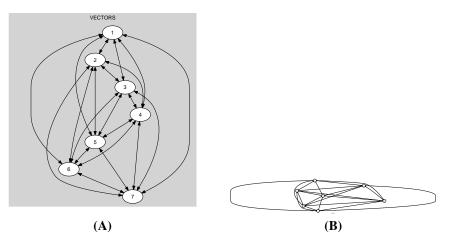


Figure 5.22: Initial and final graph of the all\_incomparable constraint