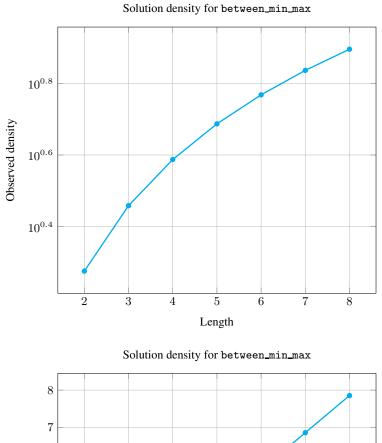
5.50 between_min_max

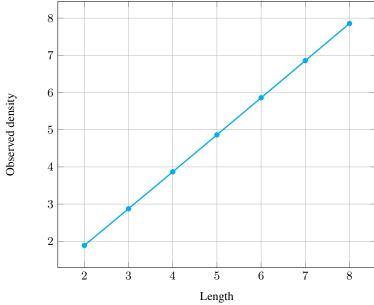
	DESCRIPTION	LINKS	GRAPH	AUTOMATON
Origin	Used for defining cumulative	_convex.		
Constraint	between_min_max(VAR,VARIA	ABLES)		
Arguments	VAR : dvar VARIABLES : collectio	n(var-dvar)		
Restrictions	$\frac{\texttt{required}(\texttt{VARIABLES},\texttt{var})}{ \texttt{VARIABLES} > 0}$			
Purpose	VAR is greater than or equal to than or equal to at least one va			S and less
Example	$(3, \langle 1, 1, 4, 8 \rangle)$ $(1, \langle 1, 1, 4, 8 \rangle)$ $(8, \langle 1, 1, 4, 8 \rangle)$ The first between_min_max than or equal to the minimum view.		e	6
	or equal to the maximum value	of $(1, 1, 4, 8)$.		
Typical	VARIABLES > 1 range(VARIABLES.var) > 1	L		
Symmetries	 Items of VARIABLES are VAR can be set to any value 			
Arg. properties	Extensible wrt. VARIABLES.			
Reformulation	By introducing two extra variab constraint can be expressed in to minimum(MIN, VARIABLES), maximum(MAX, VARIABLES), VAR \geq MIN, VAR \leq MAX.			
Counting				

-	Length (n)	2	3	4	5	6	7	8
ſ	Solutions	17	184	2417	37806	689201	14376608	338051265

Number of solutions for between_min_max: domains 0..n

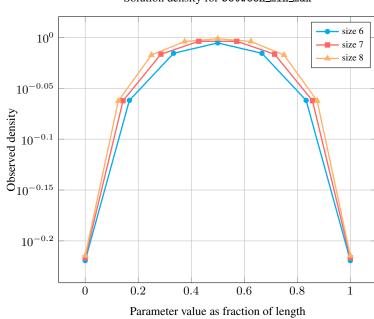
710



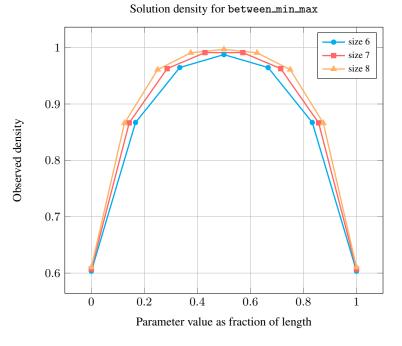


Length (n)		2	3	4	5	6	7	8
Total		17	184	2417	37806	689201	14376608	338051265
	0	5	37	369	4651	70993	1273609	26269505
	1	7	55	543	6751	102023	1817215	37281919
	2	5	55	593	7501	113489	2018899	41366849
Parameter	3	-	37	543	7501	116191	2078581	42649535
value	4	-	-	369	6751	113489	2078581	42915649
value	5	-	-	-	4651	102023	2018899	42649535
	6	-	-	-	-	70993	1817215	41366849
	7	-	-	-	-	-	1273609	37281919
	8	-	-	-	-	-	-	26269505

Solution count for between_min_max: domains 0..n



Solution density for between_min_max



Used in	cumulative_convex.					
See also	<pre>implied by: and, deepest_valley, first_value_diff_0, highest_peak, in, maximum, minimum.</pre>					
Keywords	characteristic of a constraint:automaton,automaton without counters,reified automaton constraint.constraint network structure:centered cyclic(1) constraint network(1).					

Derived Collection				
	<pre>col(ITEM-collection(var-dvar),[item(var - VAR)])</pre>			
Arc input(s)	ITEM VARIABLES			
Arc generator	<pre>PRODUCT → collection(item, variables)</pre>			
Arc arity	2			
Arc constraint(s)	$item.var \geq variables.var$			
Graph property(ies)	$\mathbf{NARC} \ge 1$			
Graph class	• ACYCLIC • BIPARTITE • NO_LOOP			
Arc input(s)	ITEM VARIABLES			
Arc generator	$PRODUCT \mapsto \texttt{collection}(\texttt{item}, \texttt{variables})$			
Arc arity	2			
Arc constraint(s)	$item.var \leq variables.var$			
Graph property(ies)	$\mathbf{NARC} \ge 1$			
Graph class	• ACYCLIC • BIPARTITE • NO_LOOP			

Graph model

Parts (A) and (B) of Figure 5.113 respectively show the initial and final graph associated with the second graph constraint of the first example of the **Example** slot. Since we use the **NARC** graph property, the two arcs of the final graph are stressed in bold. The constraint holds since 3 is greater than 1 and since 3 is less than 8.

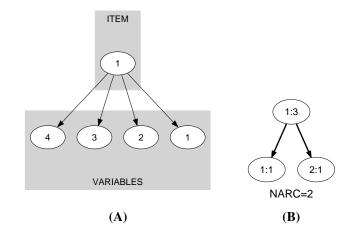


Figure 5.113: Initial and final graph of the between_min_max constraint

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Automaton

Figure 5.114 depicts the automaton associated with the between_min_max constraint. To each pair (VAR, VAR_i), where VAR_i is a variable of the collection VARIABLES corresponds a signature variable S_i . The following signature constraint links VAR, VAR_i and S_i : (VAR < VAR_i $\Leftrightarrow S_i = 0$) \land (VAR = VAR_i $\Leftrightarrow S_i = 1$) \land (VAR > VAR_i $\Leftrightarrow S_i = 2$).

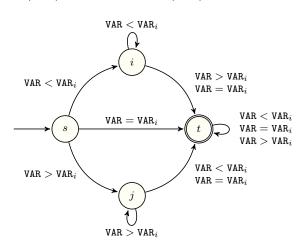


Figure 5.114: Automaton of the between_min_max constraint

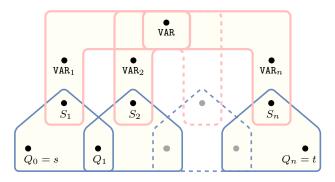


Figure 5.115: Hypergraph of the reformulation corresponding to the automaton of the between_min_max constraint