5.110 decreasing

DESCRIPTION LINKS GRAPH AUTOMATON

Origin Inspired by increasing.

Constraint decreasing(VARIABLES)

Argument VARIABLES : collection(var-dvar)

Restriction required(VARIABLES, var)

Purpose The variables of the collection VARIABLES are decreasing.

Example $(\langle 8,4,1,1\rangle)$

The decreasing constraint holds since $8 \ge 4 \ge 1 \ge 1$.

Typical |VARIABLES| > 2

range(VARIABLES.var) > 1

Symmetry One and the same constant can be added to the var attribute of all items of VARIABLES.

Arg. properties Contractible wrt. VARIABLES.

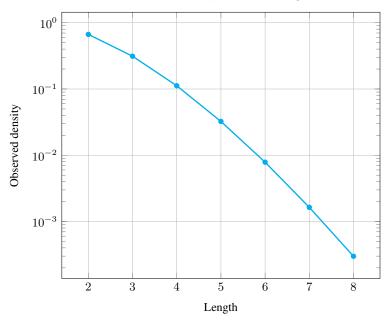
Counting

Length (n)	2	3	4	5	6	7	8
Solutions	6	20	70	252	924	3432	12870

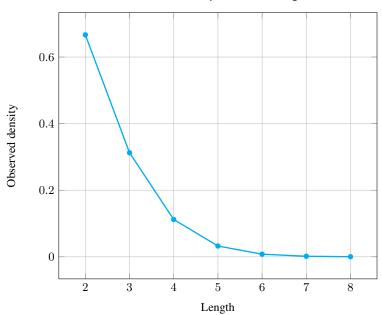
Number of solutions for decreasing: domains 0..n

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Solution density for decreasing



Solution density for decreasing



Systems increasing NValue in Choco, rel in Gecode, decreasing in MiniZinc.

See also common keyword: strictly_increasing (order constraint).

comparison swapped: increasing.

implied by: all_equal, strictly_decreasing.

implies: multi_global_contiguity, no_peak, no_valley.

Keywords

characteristic of a constraint: automaton, automaton without counters,

reified automaton constraint.

constraint network structure: sliding cyclic(1) constraint network(1).

constraint type: decomposition, order constraint.

filtering: arc-consistency.

final graph structure: acyclic, bipartite, no loop.

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 Arc input(s)
 VARIABLES

 Arc generator
 PATH → collection (variables1, variables2)

 Arc arity
 2

 Arc constraint(s)
 variables1.var ≥ variables2.var

 Graph property(ies)
 NARC= |VARIABLES| - 1

 Graph class
 • ACYCLIC

 • BIPARTITE
 • NO_LOOP

Graph model

Parts (A) and (B) of Figure 5.242 respectively show the initial and final graph associated with the **Example** slot. Since we use the **NARC** graph property, the arcs of the final graph are stressed in bold.

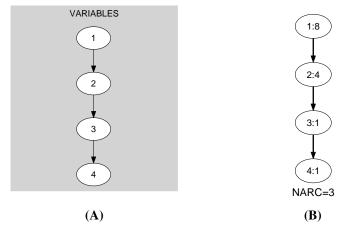


Figure 5.242: Initial and final graph of the decreasing constraint

Automaton

Figure 5.243 depicts the automaton associated with the decreasing constraint. To each pair of consecutive variables (VAR $_i$, VAR $_{i+1}$) of the collection VARIABLES corresponds a 0-1 signature variable S_i . The following signature constraint links VAR $_i$, VAR $_{i+1}$ and S_i : VAR $_i \geq$ VAR $_{i+1} \Leftrightarrow S_i$.



Figure 5.243: Automaton of the decreasing constraint

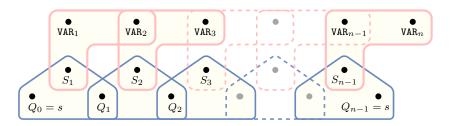


Figure 5.244: Hypergraph of the reformulation corresponding to the automaton of the decreasing constraint

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