

5.146 elements

	DESCRIPTION	LINKS	GRAPH
Origin	Derived from element .		
Constraint	<code>elements(ITEMS, TABLE)</code>		
Arguments	ITEMS : <code>collection(index-dvar, value-dvar)</code> TABLE : <code>collection(index-int, value-dvar)</code>		
Restrictions	<code>required(ITEMS, [index, value])</code> <code>ITEMS.index ≥ 1</code> <code>ITEMS.index ≤ TABLE </code> <code>required(TABLE, [index, value])</code> <code>TABLE.index ≥ 1</code> <code>TABLE.index ≤ TABLE </code> <code>distinct(TABLE, index)</code>		
Purpose	All the items of ITEMS should be equal to one of the entries of the table TABLE.		
Example	$\left(\begin{array}{l} \langle \text{index} - 4 \text{ value} - 9, \text{index} - 1 \text{ value} - 6 \rangle, \\ \langle \text{index} - 1 \text{ value} - 6, \\ \text{index} - 2 \text{ value} - 9, \\ \text{index} - 3 \text{ value} - 2, \\ \text{index} - 4 \text{ value} - 9 \rangle \end{array} \right)$		
	The <code>elements</code> constraint holds since each item of its first argument ITEMS corresponds to an item of the TABLE collection: the first item <code>⟨index - 4 value - 9⟩</code> of ITEMS corresponds to the fourth item of TABLE, while the second item <code>⟨index - 1 value - 6⟩</code> of ITEMS corresponds to the first item of TABLE.		
Typical	<code> ITEMS > 1</code> <code>range(ITEMS.index) > 1</code> <code> TABLE > 1</code> <code>range(TABLE.value) > 1</code>		
Symmetries	<ul style="list-style-type: none"> • Items of ITEMS are permutable. • Items of TABLE are permutable. • All occurrences of two distinct values in ITEMS.value or TABLE.value can be swapped; all occurrences of a value in ITEMS.value or TABLE.value can be renamed to any unused value. 		
Arg. properties	Functional dependency: ITEMS.value determined by ITEMS.index and TABLE.		

Usage	Used for replacing several <code>element</code> constraints sharing exactly the same table by a single constraint.
Reformulation	The <code>elements</code> (\langle index - I_1 value - V_1 , index - I_2 value - V_2 , ..., index - $I_{ ITEMS }$ value - $V_{ ITEMS }$ \rangle , TABLE) constraint can be expressed in term of a conjunction of $ ITEMS $ <code>elem</code> constraints of the form: <code>elem</code> (\langle index - I_1 value - V_1 \rangle , TABLE), <code>elem</code> (\langle index - I_2 value - V_2 \rangle , TABLE), ... <code>elem</code> (\langle index - $I_{ ITEMS }$ value - $V_{ ITEMS }$ \rangle , TABLE).
See also	implied by: <code>elem</code> , <code>elements_alldifferent</code> . part of system of constraints: <code>elem</code> , <code>element</code> .
Keywords	constraint arguments: pure functional dependency. constraint type: data constraint, system of constraints. filtering: arc-consistency. modelling: table, shared table, functional dependency.
Cond. implications	<code>elements</code> (ITEMS, TABLE) with <code>distinct</code> (ITEMS, index) and TABLE.value ≥ 0 implies <code>bin_packing_capa</code> (TABLE, ITEMS).

Arc input(s)	ITEMS TABLE
Arc generator	<i>PRODUCT</i> \mapsto <code>collection(items, table)</code>
Arc arity	2
Arc constraint(s)	<ul style="list-style-type: none"> • <code>items.index = table.index</code> • <code>items.value = table.value</code>
Graph property(ies)	<u>NARC</u> = ITEMS

Graph model

Parts (A) and (B) of Figure 5.320 respectively show the initial and final graph associated with the **Example** slot. Since we use the NARC graph property, the arcs of the final graph are stressed in bold.

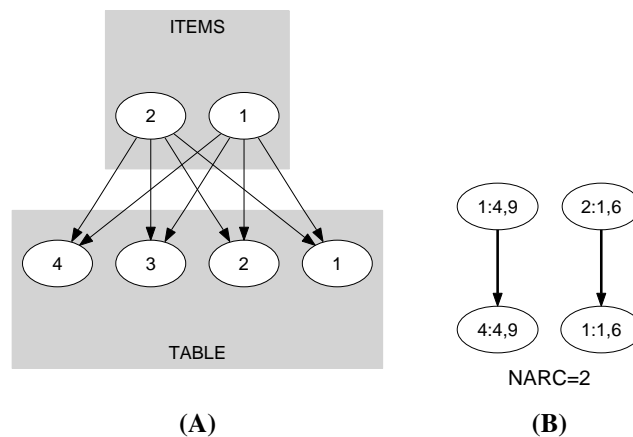


Figure 5.320: Initial and final graph of the `elements` constraint

Signature

Since all the `index` attributes of `TABLE` collection are distinct and because of the first condition `items.index = table.index` of the arc constraint, a source vertex of the final graph can have at most one successor. Therefore |ITEMS| is the maximum number of arcs of the final graph and we can rewrite $\text{NARC} = |\text{ITEMS}|$ to $\text{NARC} \geq |\text{ITEMS}|$. So we can simplify NARC to NARC.

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