## 5.148 elements\_sparse

DESCRIPTION LINKS GRAPH

Origin

Derived from element\_sparse.

Constraint

elements\_sparse(ITEMS, TABLE, DEFAULT)

Arguments

```
ITEMS : collection(index-dvar, value-dvar)
TABLE : collection(index-int, value-int)
DEFAULT : int
```

Restrictions

```
required(ITEMS,[index,value])
ITEMS.index > 1
required(TABLE,[index,value])
TABLE.index > 1
distinct(TABLE,index)
```

Purpose

All the items of ITEMS should be equal to one of the entries of the table TABLE or to the default value DEFAULT if the entry ITEMS.index does not occurs among the values of the index attribute of the TABLE collection.

Example

```
\left(\begin{array}{cccc} \left\langle\begin{array}{cccc} \text{index} - 8 & \text{value} - 9, \\ \text{index} - 3 & \text{value} - 5, \\ \text{index} - 2 & \text{value} - 5 \\ \end{array}\right\rangle, \\ \text{index} - 1 & \text{value} - 6, \\ \left\langle\begin{array}{cccc} \text{index} - 2 & \text{value} - 5, \\ \text{index} - 4 & \text{value} - 2, \\ \text{index} - 8 & \text{value} - 9 \end{array}\right\rangle, 5
```

The elements\_sparse constraint holds since:

- The first and third items (items  $\langle \mathtt{index} 8 \mathtt{value} 9 \rangle$  and  $\langle \mathtt{index} 2 \mathtt{value} 5 \rangle$ ) of its ITEMS collection respectively correspond to the fourth and second item of its TABLE collection.
- The index attribute of the second item of its ITEMS collection (i.e., value 3) does not correspond to any index of the TABLE collection. Therefore the value attribute of the second item of the ITEMS collection is set the the default value 5 given by the last argument of the elements\_sparse constraint.

**Typical** 

```
\begin{split} |\mathtt{ITEMS}| &> 1 \\ \mathtt{range}(\mathtt{ITEMS.value}) &> 1 \\ |\mathtt{TABLE}| &> 1 \\ \mathtt{range}(\mathtt{TABLE.value}) &> 1 \end{split}
```

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**Symmetries** 

- Items of ITEMS are permutable.
- Items of TABLE are permutable.

All occurrences of two distinct values in ITEMS.value, TABLE.value or DEFAULT
can be swapped; all occurrences of a value in ITEMS.value, TABLE.value or
DEFAULT can be renamed to any unused value.

Usage

Used for replacing several **element** constraints sharing exactly the same sparse table by a single constraint.

Reformulation

Let  $I_k$  and  $V_k$  respectively denote ITEMS[k].index and ITEMS[k].value ( $k \in [1, |ITEMS|[])$ ). The elements\_sparse(ITEMS, TABLE, DEFAULT) constraint can be expressed in term of |ITEMS|[ reified constraints of the form:

```
\begin{split} &((\mathbf{I}_k = \mathtt{TABLE}[1].\mathtt{index} \wedge \mathtt{V}_k = \mathtt{TABLE}[1].\mathtt{value}) \vee \\ &(\mathbf{I}_k = \mathtt{TABLE}[2].\mathtt{index} \wedge \mathtt{V}_k = \mathtt{TABLE}[2].\mathtt{value}) \vee \\ &\dots \\ &(\mathbf{I}_k = \mathtt{TABLE}[|\mathtt{TABLE}|].\mathtt{index} \wedge \mathtt{V}_k = \mathtt{TABLE}[\mathtt{TABLE}|].\mathtt{value})) \vee \\ &((\mathbf{I}_k \neq \mathtt{TABLE}[1].\mathtt{index}) \wedge \\ &(\mathbf{I}_k \neq \mathtt{TABLE}[2].\mathtt{index}) \wedge \\ &\dots \\ &(\mathbf{I}_k \neq \mathtt{TABLE}[|\mathtt{TABLE}|].\mathtt{index}) \wedge \\ &(\mathtt{V}_k = \mathtt{DEFAULT})). \end{split}
```

See also

common keyword: elem, element (data constraint), element\_sparse (sparse table).

implied by: element\_sparse.

part of system of constraints: element\_sparse.

Keywords

characteristic of a constraint: derived collection.

constraint type: data constraint, system of constraints.

filtering: arc-consistency.

modelling: table, shared table, sparse table, sparse functional dependency.

## **Derived Collections**

Arc input(s)

Arc arity

Arc generator

Arc constraint(s)

```
DEF-collection(index-int, value-int),
                       col
                             [item(index - 0, value - DEFAULT)]
                             TABLE_DEF-collection(index-dvar, value-dvar),
                       col
                                item(index - TABLE.index, value - TABLE.index),
                                item(index - DEF.index, value - DEF.value)
                     ITEMS TABLE_DEF
                       PRODUCT→collection(items, table_def)
                       • items.value = table_def.value
                       ullet items.index = table_def.index \lor table_def.index = 0
Graph property(ies)
                       NSOURCE= |ITEMS|
```

## Graph model

An item of the ITEMS collection may have up to two successors (see for instance the third item of the ITEMS collection of the Example slot). Therefore we use the graph property **NSOURCE** = |ITEMS| for enforcing the fact that each item of the ITEMS collection has at least one successor.

Parts (A) and (B) of Figure 5.324 respectively show the initial and final graph associated with the Example slot. Since we use the NSOURCE graph property, the vertices of the final graph are drawn with a double circle.

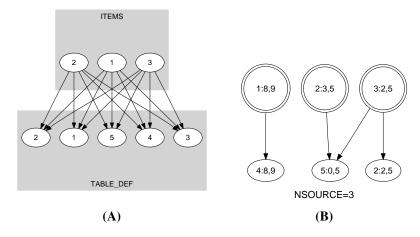


Figure 5.324: Initial and final graph of the elements\_sparse constraint

## Signature

On the one hand note that ITEMS is equal to the number of sources of the initial graph. On the other hand note that, in the initial graph, all the vertices that are not sources correspond to sinks. Since isolated vertices are eliminated from the final graph the sinks of the initial graph cannot become sources of the final graph. Therefore the maximum number of sources of the final graph is equal to ITEMS. We can rewrite NSOURCE = |ITEMS| to  $NSOURCE \ge |ITEMS|$  and simplify  $\overline{NSOURCE}$  to  $\overline{NSOURCE}$ .

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