

## 5.159 geost

	DESCRIPTION	LINKS
<b>Origin</b>	Generalisation of <a href="#">diffn</a> .	
<b>Constraint</b>	<code>geost(K, OBJECTS, SBOXES)</code>	
<b>Types</b>	VARIABLES : <a href="#">collection</a> ( <code>v-dvar</code> ) INTEGERS : <a href="#">collection</a> ( <code>v-int</code> ) POSITIVES : <a href="#">collection</a> ( <code>v-int</code> )	
<b>Arguments</b>	K : <a href="#">int</a> OBJECTS : <a href="#">collection</a> ( <code>oid-int</code> , <code>sid-dvar</code> , <code>x - VARIABLES</code> ) SBOXES : <a href="#">collection</a> ( <code>sid-int</code> , <code>t - INTEGERS</code> , <code>l - POSITIVES</code> )	
<b>Restrictions</b>	<code> VARIABLES  ≥ 1</code> <code> INTEGERS  ≥ 1</code> <code> POSITIVES  ≥ 1</code> <a href="#">required</a> (VARIABLES, <code>v</code> ) <code> VARIABLES  = K</code> <a href="#">required</a> (INTEGERS, <code>v</code> ) <code> INTEGERS  = K</code> <a href="#">required</a> (POSITIVES, <code>v</code> ) <code> POSITIVES  = K</code> <code>POSITIVES.v &gt; 0</code> <code>K &gt; 0</code> <a href="#">required</a> (OBJECTS, [ <code>oid</code> , <code>sid</code> , <code>x</code> ]) <a href="#">distinct</a> (OBJECTS, <code>oid</code> ) <code>OBJECTS.oid ≥ 1</code> <code>OBJECTS.oid ≤  OBJECTS </code> <code>OBJECTS.sid ≥ 1</code> <code>OBJECTS.sid ≤  SBOXES </code> <code> SBOXES  ≥ 1</code> <a href="#">required</a> (SBOXES, [ <code>sid</code> , <code>t</code> , <code>l</code> ]) <code>SBOXES.sid ≥ 1</code> <code>SBOXES.sid ≤  SBOXES </code> <a href="#">do_not_overlap</a> (SBOXES)	

**Purpose**

Holds if, for each pair of objects  $(O_i, O_j)$ ,  $i < j$ ,  $O_i$  and  $O_j$  do not overlap with respect to a set of dimensions  $\{1, 2, \dots, K\}$ .  $O_i$  and  $O_j$  are objects that take a shape among a set of shapes. Each *shape* is defined as a finite set of shifted boxes, where each shifted box is described by a box in a K-dimensional space at a given offset (from the origin of the shape) with given sizes that are all strictly greater than 0. More precisely, a *shifted box* is an entity defined by its shape id *sid*, shift offset *t*, and sizes *l*. Then, a shape is defined as the union of shifted boxes sharing the same shape id. An *object* is an entity defined by its unique object identifier *oid*, shape id *sid* and origin *x*.

An object  $O_i$  *does not overlap* an object  $O_j$  with respect to the set of dimensions  $\{1, 2, \dots, K\}$  if and only if for all shifted box  $s_i$  associated with  $O_i$  and for all shifted box  $s_j$  associated with  $O_j$  there exists a dimension  $d \in \{1, 2, \dots, K\}$  such that the start of  $s_i$  in dimension  $d$  is greater than or equal to the end of  $s_j$  in dimension  $d$ , or the start of  $s_j$  in dimension  $d$  is greater than or equal to the end of  $s_i$  in dimension  $d$ .

**Example**

2,	$\left\langle \begin{array}{l} \text{oid} - 1 \quad \text{sid} - 1 \quad \mathbf{x} - \langle 1, 2 \rangle, \\ \text{oid} - 2 \quad \text{sid} - 5 \quad \mathbf{x} - \langle 2, 1 \rangle, \\ \text{oid} - 3 \quad \text{sid} - 8 \quad \mathbf{x} - \langle 4, 1 \rangle \end{array} \right\rangle,$
	$\text{sid} - 1 \quad \mathbf{t} - \langle 0, 0 \rangle \quad \mathbf{l} - \langle 2, 1 \rangle,$
	$\text{sid} - 1 \quad \mathbf{t} - \langle 0, 1 \rangle \quad \mathbf{l} - \langle 1, 2 \rangle,$
	$\text{sid} - 1 \quad \mathbf{t} - \langle 1, 2 \rangle \quad \mathbf{l} - \langle 3, 1 \rangle,$
	$\text{sid} - 2 \quad \mathbf{t} - \langle 0, 0 \rangle \quad \mathbf{l} - \langle 3, 1 \rangle,$
	$\text{sid} - 2 \quad \mathbf{t} - \langle 0, 1 \rangle \quad \mathbf{l} - \langle 1, 3 \rangle,$
	$\text{sid} - 2 \quad \mathbf{t} - \langle 2, 1 \rangle \quad \mathbf{l} - \langle 1, 1 \rangle,$
	$\text{sid} - 3 \quad \mathbf{t} - \langle 0, 0 \rangle \quad \mathbf{l} - \langle 2, 1 \rangle,$
	$\text{sid} - 3 \quad \mathbf{t} - \langle 1, 1 \rangle \quad \mathbf{l} - \langle 1, 2 \rangle,$
	$\text{sid} - 3 \quad \mathbf{t} - \langle -2, 2 \rangle \quad \mathbf{l} - \langle 3, 1 \rangle,$
	$\left\langle \begin{array}{l} \text{sid} - 4 \quad \mathbf{t} - \langle 0, 0 \rangle \quad \mathbf{l} - \langle 3, 1 \rangle, \\ \text{sid} - 4 \quad \mathbf{t} - \langle 0, 1 \rangle \quad \mathbf{l} - \langle 1, 1 \rangle, \\ \text{sid} - 4 \quad \mathbf{t} - \langle 2, 1 \rangle \quad \mathbf{l} - \langle 1, 3 \rangle, \\ \text{sid} - 5 \quad \mathbf{t} - \langle 0, 0 \rangle \quad \mathbf{l} - \langle 2, 1 \rangle, \\ \text{sid} - 5 \quad \mathbf{t} - \langle 1, 1 \rangle \quad \mathbf{l} - \langle 1, 1 \rangle, \\ \text{sid} - 5 \quad \mathbf{t} - \langle 0, 2 \rangle \quad \mathbf{l} - \langle 2, 1 \rangle, \\ \text{sid} - 6 \quad \mathbf{t} - \langle 0, 0 \rangle \quad \mathbf{l} - \langle 3, 1 \rangle, \\ \text{sid} - 6 \quad \mathbf{t} - \langle 0, 1 \rangle \quad \mathbf{l} - \langle 1, 1 \rangle, \\ \text{sid} - 6 \quad \mathbf{t} - \langle 2, 1 \rangle \quad \mathbf{l} - \langle 1, 1 \rangle, \\ \text{sid} - 7 \quad \mathbf{t} - \langle 0, 0 \rangle \quad \mathbf{l} - \langle 3, 2 \rangle, \\ \text{sid} - 8 \quad \mathbf{t} - \langle 0, 0 \rangle \quad \mathbf{l} - \langle 2, 3 \rangle \end{array} \right\rangle$

Parts (A), (B) and (C) of Figure 5.349 respectively represent the potential shapes associated with the three objects of the example. Part (D) shows the position of the three objects of the example, where the first, second and third objects were respectively assigned shapes 1, 5 and 8. The coordinates of the leftmost lowest corner of each object are stressed in bold. The *geost* constraint holds since the three objects do not overlap (i.e., see part (D) if Figure 5.349).

**Typical**

$|\text{OBJECTS}| > 1$

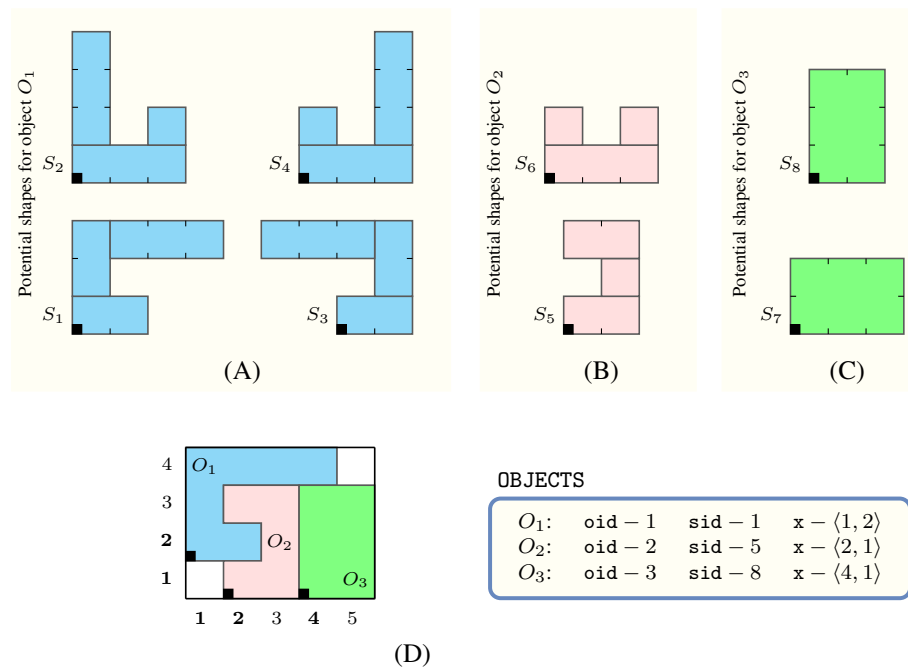


Figure 5.349: (D) The three non-overlapping objects  $O_1$ ,  $O_2$ ,  $O_3$  of the **Example** slot respectively assigned shapes  $S_1$ ,  $S_5$ ,  $S_8$ ; (A), (B), (C) shapes  $S_1$ ,  $S_2$ ,  $S_3$ ,  $S_4$ ,  $S_5$ ,  $S_6$ ,  $S_7$  and  $S_8$  are respectively made up from 3, 3, 3, 3, 3, 3, 1 and 1 disjoint shifted box.

### Symmetries

- Items of **OBJECTS** are [permutable](#).
- Items of **SBOXES** are [permutable](#).
- Items of **OBJECTS.x**, **SBOXES.t** and **SBOXES.l** are [permutable](#) (*same permutation used*).
- **SBOXES.l.v** can be [decreased](#) to any value  $\geq 1$ .

### Usage

The `geost` constraint allows to model directly a large number of placement problems.

### Remark

In the two-dimensional case, when rectangles heights are all equal to one and when rectangles starts in the first dimension are all fixed, the `geost` constraint can be rewritten as a `k_alldifferent` constraint corresponding to a system of `alldifferent` constraints derived from the maximum cliques of the corresponding interval graph.

### Algorithm

A [sweep-based](#) filtering algorithm for this constraint is described in [38]. Unlike previous sweep filtering algorithms which move a line for finding a feasible position for the origin of an object, this algorithm performs a recursive traversal of the multidimensional placement space. It explores all points of the domain of the origin of the object under focus, one by one, in increasing lexicographic order, until a point is found that is not infeasible for any non-overlapping constraints. To make the search efficient, instead of moving each time

to the successor point, the search is arranged so that it skips points that are known to be infeasible for some non-overlapping constraint.

Within the context of breaking symmetries six different ways of integrating within `geost` a chain of lexicographical ordering constraints like `lex_chain_less` for enforcing a lexicographic ordering on the origin coordinates of identical objects, are described in [3].

#### Systems

`geost` in **Choco**, `geost` in **JaCoP**, `geost` in **SICStus**.

#### See also

**common keyword:** `calendar` (*multi-site employee scheduling with calendar constraints, scheduling with machine choice, calendars and preemption*), `diffn` (*geometrical constraint, non-overlapping*), `lex_chain_less`, `lex_chain_lesseq` (*symmetry*), `non_overlap_sboxes` (*geometrical constraint, non-overlapping*), `visible` (*geometrical constraint, sweep*).

**generalisation:** `geost_time` (*temporal dimension added to geometrical dimensions*).

**specialisation:** `k_alldifferent` (*when rectangles heights are all equal to 1 and rectangles starts in the first dimension are all fixed*), `lex_alldifferent` (*object replaced by vector*).

#### Keywords

**application area:** floor planning problem.

**combinatorial object:** pentomino.

**constraint arguments:** business rules.

**constraint type:** logic, decomposition, timetabling constraint, predefined constraint, relaxation.

**filtering:** sweep.

**geometry:** geometrical constraint, non-overlapping.

**heuristics:** heuristics for two-dimensional rectangle placement problems.

**modelling:** multi-site employee scheduling with calendar constraints, scheduling with machine choice, calendars and preemption, disjunction, assignment dimension, assigning and scheduling tasks that run in parallel, assignment to the same set of values, relaxation dimension.

**modelling exercises:** multi-site employee scheduling with calendar constraints, scheduling with machine choice, calendars and preemption, assigning and scheduling tasks that run in parallel, assignment to the same set of values, relaxation dimension.

**problems:** strip packing, two-dimensional orthogonal packing, pallet loading.

**puzzles:** squared squares, packing almost squares, Partridge, pentomino, Shikaku, smallest square for packing consecutive dominoes, smallest square for packing rectangles with distinct sizes, smallest rectangle area, Conway packing problem.

**symmetry:** symmetry.