$\overline{\mathbf{NARC}}$, PRODUCT; AUTOMATON

5.177 in

	DESCRIPTION	LINKS	GRAPH	AUTOMATON
Origin	Domain definition.			
Constraint	in(VAR, VALUES)			
Synonyms	dom, in_set, member.			
Arguments	VAR : dvar VALUES : collection(val-	-int)		
Restrictions	<pre> VALUES > 0 required(VALUES,val) distinct(VALUES,val)</pre>			
Purpose	Enforce the domain variable VAR VALUES collection.	a to take a value withi	n the values described	by the
Example	$(3, \langle 1, 3 \rangle)$ The in constraint holds since its tion of values VALUES = $\langle 1, 3 \rangle$.	first argument VAR =	= 3 occurs within the	collec-
Typical	VALUES > 1			
Symmetries	 Items of VALUES are permute VAR can be set to any value One and the same constant all items of VALUES. 	table. of VALUES.val. can be added to VAR as	s well as to the val attri	bute of
Arg. properties	Extensible wrt. VALUES.			
Remark	Entailment occurs immediately after The in constraint is called dom in MiniZinc (http://www.minizinc.or sarily fixed, i.e. it can be a domain	er posting this constrain Gecode (http://www.g g/). In MiniZinc the v variable.	tt. ecode.org/), and member ral attribute is not neces	in ;-
Systems	member in Choco, rel in Gecode in in SICStus, in_set in SICStu	e, domin Gecode, in in Is.	n JaCoP , member in Mi	niZinc,
Used in	among, cardinality_atmost_p in_same_partition, open_among	partition, group,	group_skip_isolate	d_item,

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See also	<pre>common keyword: domain (domain definition), in_interval, in_same_partition, in_set(value constraint).</pre>
	implied by: maximum, minimum.
	implies: between_min_max.
	negation: not_in.
Keywords	characteristic of a constraint: automaton, automaton without counters, reified automaton constraint, derived collection.
	constraint arguments: unary constraint.
	constraint network structure: centered cyclic(1) constraint network(1).
	constraint type: value constraint.
	filtering: arc-consistency.
	modelling: included, domain definition.

Arc input(s) VARTABLES VALUES
Arc generator PRODUCT \mapsto collection(variables, values)
Arc arity 2
Arc constraint(s) variables.var = values.val
Graph property(ies) NARC= 1

Parts (A) and (B) of Figure 5.398 respectively show the initial and final graph associated with the **Example** slot. Since we use the **NARC** graph property, the unique arc of the final graph is stressed in bold.



Figure 5.398: Initial and final graph of the in constraint

SignatureSince all the val attributes of the VALUES collection are distinct and because of the arc con-
straint variables.var = values.val the final graph contains at most one arc. Therefore
we can rewrite NARC = 1 to NARC \geq 1 and simplify NARC to NARC.

Graph model

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Automaton

Figure 5.399 depicts the automaton associated with the in constraint. Let VAL_i be the val attribute of the i^{th} item of the VALUES collection. To each pair (VAR, VAL_i) corresponds a 0-1 signature variable S_i as well as the following signature constraint: VAR = VAL_i $\Leftrightarrow S_i$.



Figure 5.399: Automaton of the in constraint



Figure 5.400: Hypergraph of the reformulation corresponding to the automaton of the in constraint