

5.205 **k_cut**

	DESCRIPTION	LINKS	GRAPH
Origin	E. Althaus		
Constraint	<code>k_cut(K, NODES)</code>		
Arguments	K : <code>int</code> NODES : <code>collection(index=int, succ=svar)</code>		
Restrictions	$K \geq 1$ $K \leq \text{NODES} $ <code>required(NODES, [index, succ])</code> $\text{NODES.index} \geq 1$ $\text{NODES.index} \leq \text{NODES} $ <code>distinct(NODES, index)</code> $\text{NODES.succ} \geq 1$ $\text{NODES.succ} \leq \text{NODES} $		
Purpose	Select some arcs of a digraph in order to have at least K connected components (an isolated vertex, i.e. a vertex without any ingoing or outgoing arc, is counted as one connected component).		
Example	$\left(3, \left\langle \begin{array}{ll} \text{index} - 1 & \text{succ} - \emptyset, \\ \text{index} - 2 & \text{succ} - \{3, 5\}, \\ \text{index} - 3 & \text{succ} - \{5\}, \\ \text{index} - 4 & \text{succ} - \emptyset, \\ \text{index} - 5 & \text{succ} - \{2, 3\} \end{array} \right\rangle \right)$ <p>The <code>k_cut</code> constraint holds since the graph corresponding to the <code>NODES</code> collection contains 3 connected components (i.e., two connected components respectively involving vertices 1 and 4 and a third connected component containing the remaining vertices 2, 3 and 5), and since the first argument <code>K</code> enforces to have at least 3 connected components.</p>		
Typical	$ \text{NODES} > 1$		
Symmetries	<ul style="list-style-type: none"> • <code>K</code> can be decreased to any value ≥ 1. • Items of <code>NODES</code> are permutable. 		
See also	common keyword: <code>link_set_to_booleans</code> (<i>constraint involving set variables</i>). used in graph description: <code>in_set</code> .		
Keywords	constraint arguments: constraint involving set variables. constraint type: graph constraint. filtering: linear programming. final graph structure: connected component.		

Arc input(s)	NODES
Arc generator	$CLIQUE \mapsto collection(nodes1, nodes2)$
Arc arity	2
Arc constraint(s)	$\bigvee \left(\begin{array}{l} nodes1.index = nodes2.index, \\ in_set(nodes2.index, nodes1.succ) \end{array} \right)$
Graph property(ies)	$NCC \geq K$

Graph model

$nodes1.index = nodes2.index$ holds if $nodes1$ and $nodes2$ correspond to the same vertex. It is used in order to enforce keeping all the vertices of the initial graph. This is because an isolated vertex counts always as one **connected component**. Within the context of the **Example** slot, part (A) of Figure 5.459 shows the initial graph from which we have chosen to start. It is derived from the set associated with each vertex. Each set describes the potential values of the `succ` attribute of a given vertex. Part (B) of Figure 5.459 gives the final graph associated with the example of the **Example** slot. The `k_cut` constraint holds since we have at least $K = 3$ **connected components** in the final graph.

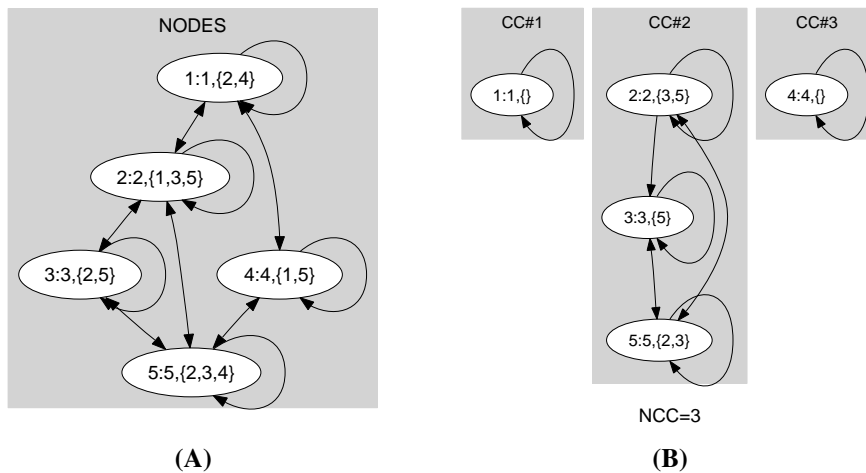


Figure 5.459: Initial and final graph of the `k_cut` set constraint