

5.233 `lex_lesseq_allperm`

	DESCRIPTION	LINKS
Origin	Inspired by [168]	
Constraint	<code>lex_lesseq_allperm(VECTOR1, VECTOR2)</code>	
Synonym	<code>leximin.</code>	
Arguments	VECTOR1 : <code>collection(var-dvar)</code> VECTOR2 : <code>collection(var-dvar)</code>	
Restrictions	<code>required(VECTOR1, var)</code> <code>required(VECTOR2, var)</code> $ \text{VECTOR1} = \text{VECTOR2} $	
Purpose	<p>VECTOR1 is <i>lexicographically less than or equal to</i> all permutations of VECTOR2. Given two vectors, \vec{X} and \vec{Y} of n components, $\langle X_0, \dots, X_{n-1} \rangle$ and $\langle Y_0, \dots, Y_{n-1} \rangle$, \vec{X} is <i>lexicographically less than or equal to</i> \vec{Y} if and only if $n = 0$ or $X_0 < Y_0$ or $X_0 = Y_0$ and $\langle X_1, \dots, X_{n-1} \rangle$ is <i>lexicographically less than or equal to</i> $\langle Y_1, \dots, Y_{n-1} \rangle$.</p>	
Example	<div style="border: 1px solid blue; padding: 5px; display: inline-block;"> $(\langle 1, 2, 3 \rangle, \langle 3, 1, 2 \rangle)$ </div> <p>The <code>lex_lesseq_allperm</code> constraint holds since vector $\langle 1, 2, 3 \rangle$ is lexicographically less than or equal to all the permutations of vector $\langle 3, 1, 2 \rangle$ (i.e., $\langle 1, 2, 3 \rangle$, $\langle 1, 3, 2 \rangle$, $\langle 2, 1, 3 \rangle$, $\langle 2, 3, 1 \rangle$, $\langle 3, 1, 2 \rangle$, $\langle 3, 2, 1 \rangle$).</p>	
Typical	$ \text{VECTOR1} > 1$	
Symmetry	All occurrences of two distinct values in <code>VECTOR1.var</code> or <code>VECTOR2.var</code> can be <code>swapped</code> ; all occurrences of a value in <code>VECTOR1.var</code> or <code>VECTOR2.var</code> can be <code>renamed</code> to any unused value.	
Arg. properties	<code>Suffix-contractible</code> wrt. <code>VECTOR1</code> and <code>VECTOR2</code> (<i>remove items from same position</i>).	
Remark	The <code>lex_lesseq_allperm(VECTOR1, VECTOR2)</code> can be reformulated as the conjunction <code>sort(VECTOR2, VECTOR)</code> , <code>lex_lesseq(VECTOR1, VECTOR)</code> .	
Systems	<code>leximin</code> in Choco .	
Used in	<code>allperm.</code>	
See also	common keyword: <code>allperm</code> (<i>matrix symmetry, lexicographic order</i>). implies: <code>lex_lesseq</code> . system of constraints: <code>allperm</code> .	

Keywords

characteristic of a constraint: vector.

constraint type: predefined constraint, order constraint.

symmetry: symmetry, matrix symmetry, lexicographic order.