

5.253 min_dist_between_inflexion

	DESCRIPTION	LINKS	AUTOMATON
Origin	Derived from <code>inflexion</code>		
Constraint	<code>min_dist_between_inflexion(MINDIST, VARIABLES)</code>		
Arguments	<p>MINDIST : <code>int</code></p> <p>VARIABLES : <code>collection(var-dvar)</code></p>		
Restrictions	<p>$MINDIST \geq 0$</p> <p>$MINDIST \leq VARIABLES$</p> <p><code>required(VARIABLES, var)</code></p>		
Purpose	<p>Given an integer value MINDIST and a sequence of variables VARIABLES enforce MINDIST to be greater than or equal to the smallest distance between two consecutive inflexions in the sequence VARIABLES, or to $VARIABLES$ if no more than one inflexion exists.</p> <p>An <i>inflexion</i> of a sequence of variables VARIABLES is a set of consecutive variables $V_i, V_{i+1}, \dots, V_{j-1}, V_j$ ($i + 1 < j$) such that one of the following conditions holds:</p> <ul style="list-style-type: none"> • $V_i < V_{i+1} \wedge V_{i+1} = \dots = V_{j-1} \wedge V_{j-1} > V_j$, • $V_i > V_{i+1} \wedge V_{i+1} = \dots = V_{j-1} \wedge V_{j-1} < V_j$. <p>In this context, the index j is the <i>position</i> of the inflexion (i.e., the first instant when the inflexion is discovered when scanning the sequence of variables VARIABLES from left to right). The <i>distance between two consecutive inflexions</i> is the absolute value of the difference of their corresponding positions.</p>		
Example	<div style="border: 1px solid blue; padding: 5px; display: inline-block;">(2, (2, 2, 3, 3, 2, 2, 1, 4, 4, 3))</div> <p>Figure 5.531 shows the three inflexions associated with the sequence 2, 2, 3, 3, 2, 2, 1, 4, 4, 3 and their respective positions 5, 8 and 10 in red. The <code>min_dist_between_inflexion</code> constraint holds since its first argument $MINDIST = 2$ is greater than or equal to the smallest distance 2 between two consecutive inflexions of the sequence of variables VARIABLES.</p>		
Typical	<p>$MINDIST > 1$</p> <p>$VARIABLES > 3$</p> <p><code>range(VARIABLES.var) > 1</code></p>		
Symmetries	<ul style="list-style-type: none"> • Items of VARIABLES can be <code>reversed</code>. • One and the same constant can be <code>added</code> to the <code>var</code> attribute of all items of VARIABLES. 		
Counting			

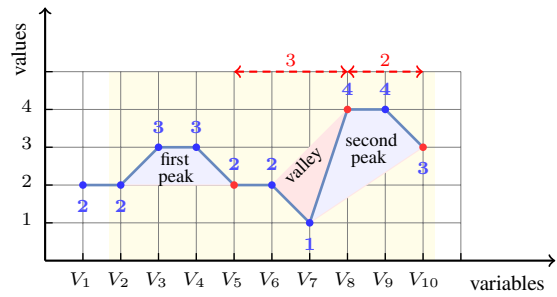
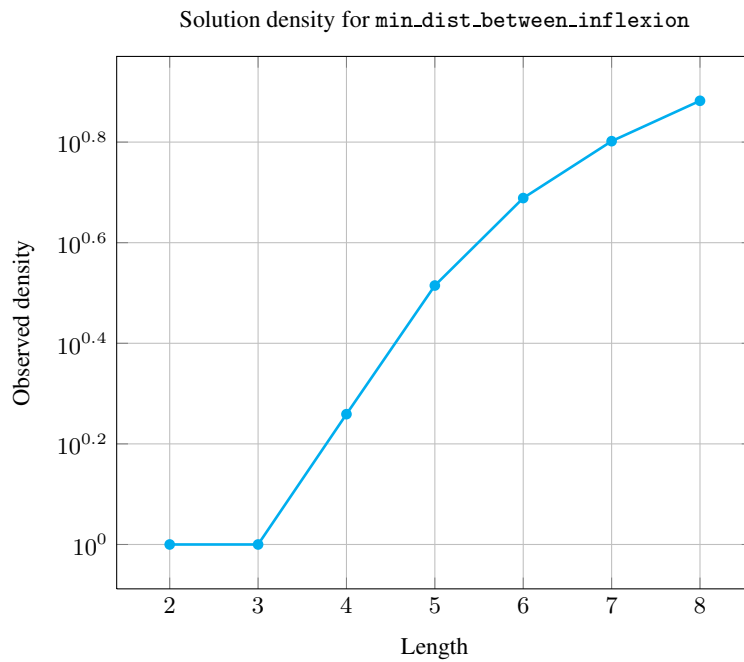
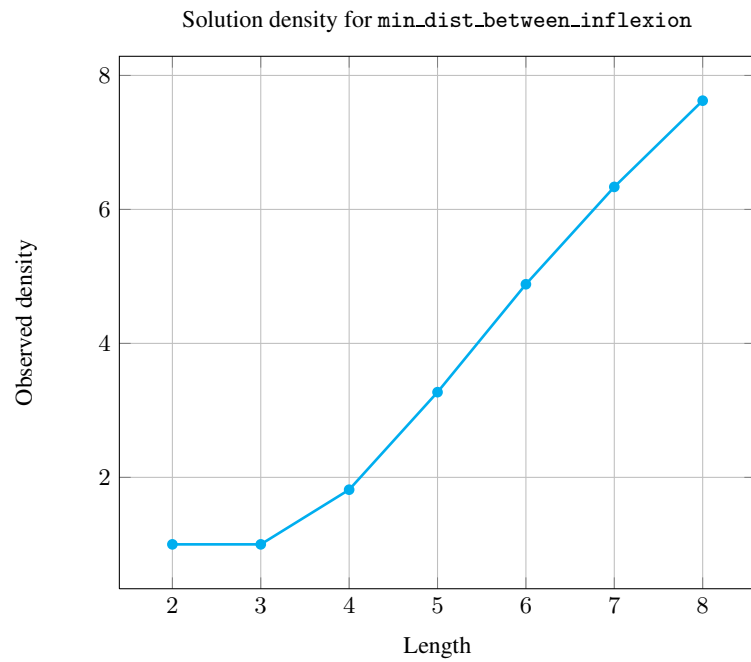


Figure 5.531: Illustration of the **Example** slot: a sequence of ten variables $V_1, V_2, V_3, V_4, V_5, V_6, V_7, V_8, V_9, V_{10}$ respectively fixed to values 2, 2, 3, 3, 2, 2, 1, 4, 4, 3 and its three inflexions, two peaks and one valley; each red point denotes an instant where a new inflexion is discovered while scanning the sequence from left to right; as shown by the rightmost arrow, the minimum distance between two consecutive inflexions is equal to 2.

Length (n)	2	3	4	5	6	7	8
Solutions	9	64	1135	25444	574483	13287476	328156407

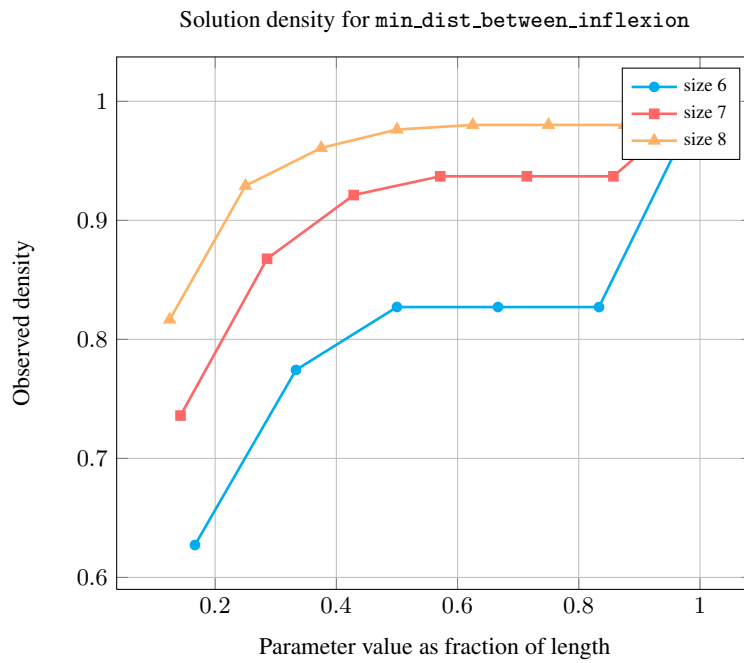
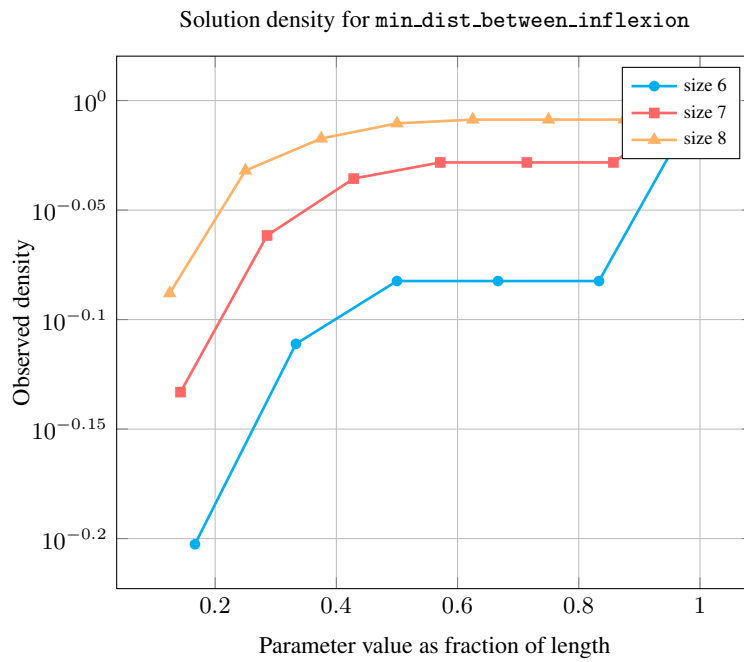
Number of solutions for min_dist_between_inflexion: domains 0..n





Length (n)		2	3	4	5	6	7	8
Total		9	64	1135	25444	574483	13287476	328156407
Parameter value	1	-	-	170	3598	73794	1543512	35152278
	2	9	-	170	4690	91098	1819764	39992562
	3	-	64	170	4690	97314	1932012	41360676
	4	-	-	625	4690	97314	1965012	42025560
	5	-	-	-	7776	97314	1965012	42192870
	6	-	-	-	-	117649	1965012	42192870
	7	-	-	-	-	-	2097152	42192870
	8	-	-	-	-	-	-	43046721

Solution count for min_dist_between_inflexion: domains 0..n



See also

common keyword: [inflexion](#), [longest_decreasing_sequence](#), [longest_increasing_sequence](#), [peak](#), [valley \(sequence\)](#).

Keywords

characteristic of a constraint: automaton, automaton with counters,
automaton with same input symbol.

combinatorial object: sequence.

constraint network structure: sliding cyclic(1) constraint network(3).

Automaton

Figure 5.532 depicts the automaton associated with the `min_dist_between_inflexion` constraint.

STATES SEMANTICS

s	: stationary mode	$(=)$
$i0$: increasing mode (no inflexion yet found)	$(< \{< =\}^*)$
$d0$: decreasing mode (no inflexion yet found)	$(> \{> =\}^*)$
$i1$: increasing mode (at least one inflexion already found)	$(< \{< =\}^*)$
$d1$: decreasing mode (at least one inflexion already found)	$(> \{> =\}^*)$

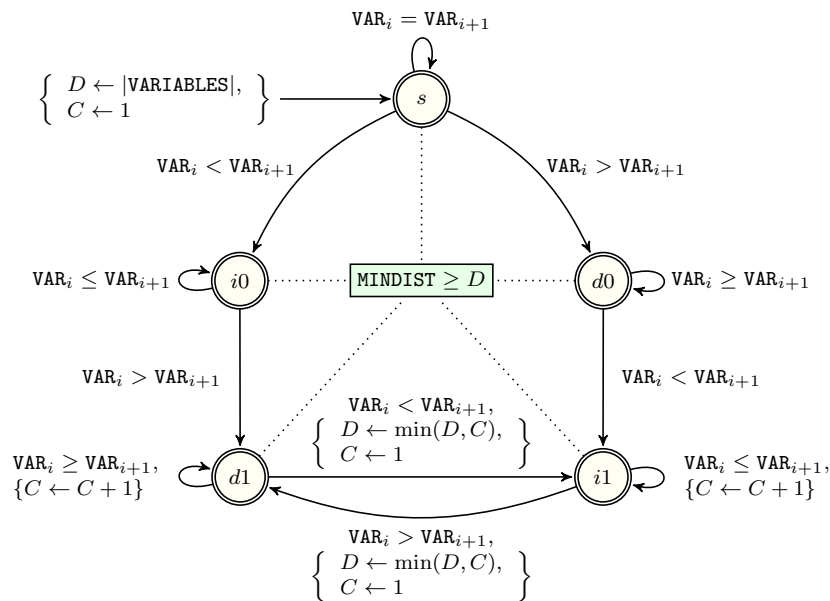


Figure 5.532: Automaton of the `min_dist_between_inflexion` constraint (state s means that we are in *stationary* mode, state $i0$ means that we are in *increasing* mode and that we did not yet found any inflexion, state $d0$ means that we are in *decreasing* mode and that we did not yet found any inflexion, state $i1$ means that we are in *increasing* mode and that we already found at least one inflexion, state $d1$ means that we are in *decreasing* mode and that we already found at least one inflexion, the minimum distance between two consecutive inflexions is updated each time we switch from $i1$ to $d1$ mode – or conversely from $d1$ to $i1$ mode – and the counter D is updated accordingly)

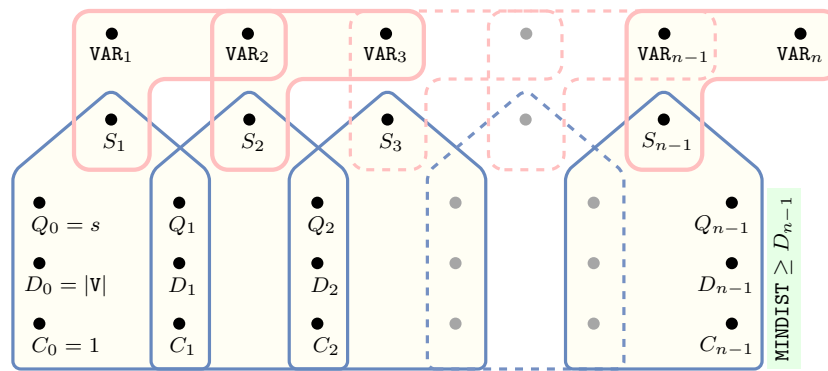


Figure 5.533: Hypergraph of the reformulation corresponding to the automaton of the `min_dist_between_inflexion` constraint where `V` is a shortcut for `VARIABLES` (since all states of the automaton are accepting there is no restriction on the last variable Q_{n-1})

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