

5.349 sliding_card_skip0

	DESCRIPTION	LINKS	GRAPH	AUTOMATON
Origin	N. Beldiceanu			
Constraint	sliding_card_skip0(ATLEAST, ATMOST, VARIABLES, VALUES)			
Arguments	ATLEAST : int ATMOST : int VARIABLES : collection(var-dvar) VALUES : collection(val-int)			
Restrictions	ATLEAST ≥ 0 ATMOST $\leq \text{VARIABLES} $ ATMOST ≥ 0 ATMOST $\leq \text{VARIABLES} $ ATMOST \geq ATLEAST required(VARIABLES, var) required(VALUES, val) distinct(VALUES, val) VALUES.val $\neq 0$			
Purpose	<p>Let n be the total number of variables of the collection VARIABLES. A <i>maximum non-zero set of consecutive variables</i> $X_i..X_j$ ($1 \leq i \leq j \leq n$) is defined in the following way:</p> <ul style="list-style-type: none"> • All variables X_i, \dots, X_j take a non-zero value, • $i = 1$ or X_{i-1} is equal to 0, • $j = n$ or X_{j+1} is equal to 0. <p>Enforces that each maximum non-zero set of consecutive variables of the collection VARIABLES contains at least ATLEAST and at most ATMOST values from the collection of values VALUES.</p>			
Example	<div style="border: 1px solid black; padding: 5px; display: inline-block;"> $(2, 3, \langle 0, 7, 2, 9, 0, 0, 9, 4, 9 \rangle, \langle 7, 9 \rangle)$ </div> <p>The sliding_card_skip0 constraint holds since the two maximum non-zero set of consecutive values 7 2 9 and 9 4 9 of its third argument $\langle 0, 7, 2, 9, 0, 0, 9, 4, 9 \rangle$ take both 2 ($2 \in [\text{ATLEAST}, \text{ATMOST}] = [2, 3]$) values within the set of values $\langle 7, 9 \rangle$.</p>			
Typical	$ \text{VARIABLES} > 1$ $ \text{VALUES} > 0$ $ \text{VARIABLES} > \text{VALUES} $ atleast(1, VARIABLES, 0) ATLEAST $> 0 \vee$ ATMOST $< \text{VARIABLES} $			

Symmetries

- ATLEAST can be **decreased** to any value ≥ 0 .
- ATMOST can be **increased** to any value $\leq |\text{VARIABLES}|$.
- Items of VARIABLES can be **reversed**.
- An occurrence of a value different from 0 of VARIABLES.var that belongs to VALUES.val (resp. does not belong to VALUES.val) can be replaced by any other value different from 0 in VALUES.val (resp. not in VALUES.val).

Usage

This constraint is useful in timetabling problems where the variables are interpreted as the type of job that a person does on consecutive days. Value 0 represents a rest day and one imposes a cardinality constraint on periods that are located between rest periods.

Remark

One cannot initially state a **global_cardinality** constraint since the rest days are not yet allocated. One can also not use an **among_seq** constraint since it does not hold for the sequences of consecutive variables that contains at least one rest day.

See also

related: **among** (*counting constraint on the full sequence*), **global_cardinality** (*counting constraint for different values on the full sequence*).

specialisation: **among_low_up** (*maximal sequences replaced by the full sequence*).

Keywords

characteristic of a constraint: automaton, automaton with counters.

combinatorial object: sequence.

constraint network structure: alpha-acyclic constraint network(2).

constraint type: timetabling constraint, sliding sequence constraint.

Arc input(s)	VARIABLES
Arc generator	$PATH \mapsto \text{collection}(\text{variables1}, \text{variables2})$ $LOOP \mapsto \text{collection}(\text{variables1}, \text{variables2})$
Arc arity	2
Arc constraint(s)	<ul style="list-style-type: none"> • $\text{variables1.var} \neq 0$ • $\text{variables2.var} \neq 0$
Sets	$CC \mapsto [\text{variables}]$
Constraint(s) on sets	<u>$\text{among_low_up}(\text{ATLEAST}, \text{ATMOST}, \text{variables}, \text{VALUES})$</u>

Graph model

Note that the arc constraint will produce the different sequences of consecutive variables that do not contain any 0. The CC set generator produces all the connected components of the final graph.

Parts (A) and (B) of Figure 5.683 respectively show the initial and final graph associated with the **Example** slot. Since we use the set generator CC we show the two connected components of the final graph. Since these two connected components both contains between 2 and 3 variables that take their values in $\{7, 9\}$ the `sliding_card_skip0` constraint holds.

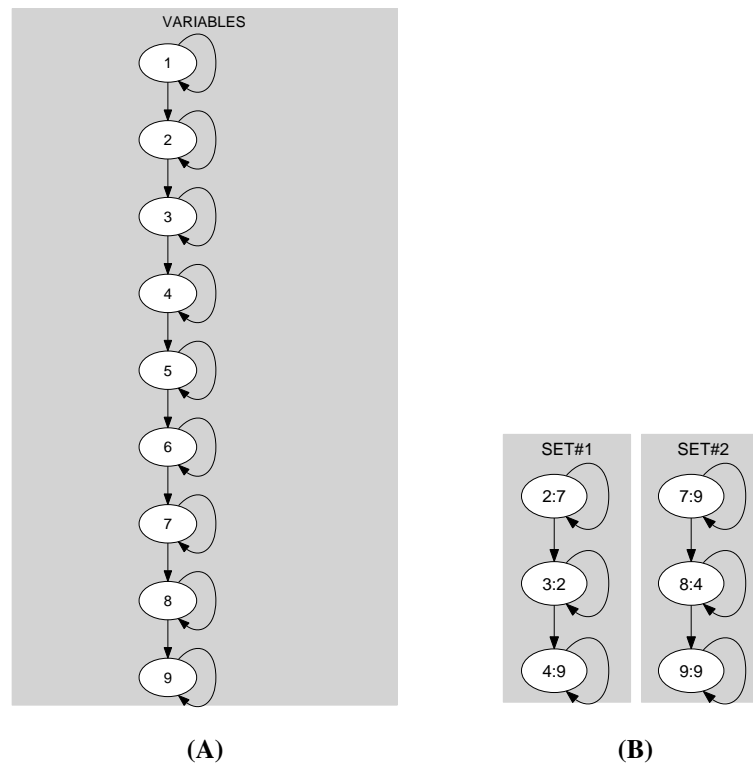


Figure 5.683: Initial and final graph of the `sliding_card_skip0` constraint

Automaton

Figure 5.684 depicts the automaton associated with the `sliding_card_skip0` constraint. To each variable VAR_i of the collection `VARIABLES` corresponds a signature variable S_i . The following signature constraint links VAR_i and S_i :

$$\begin{aligned} (VAR_i = 0) &\Leftrightarrow S_i = 0 \wedge \\ (VAR_i \neq 0 \wedge VAR_i \notin \text{VALUES}) &\Leftrightarrow S_i = 1 \wedge \\ (VAR_i \neq 0 \wedge VAR_i \in \text{VALUES}) &\Leftrightarrow S_i = 2. \end{aligned}$$

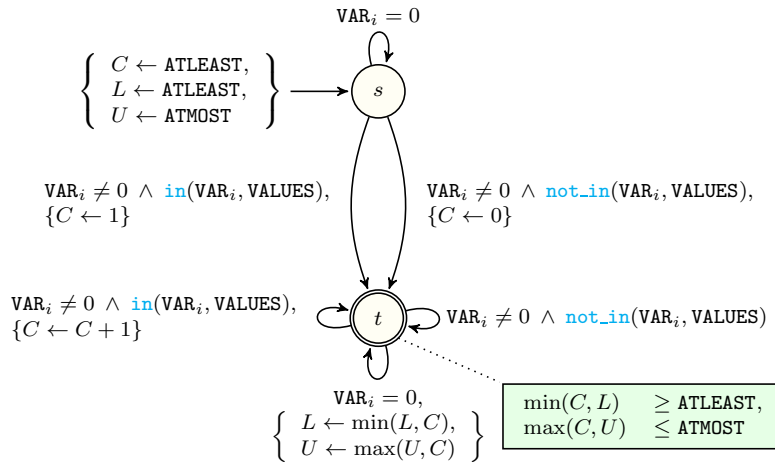


Figure 5.684: Automaton of the `sliding_card_skip0` constraint

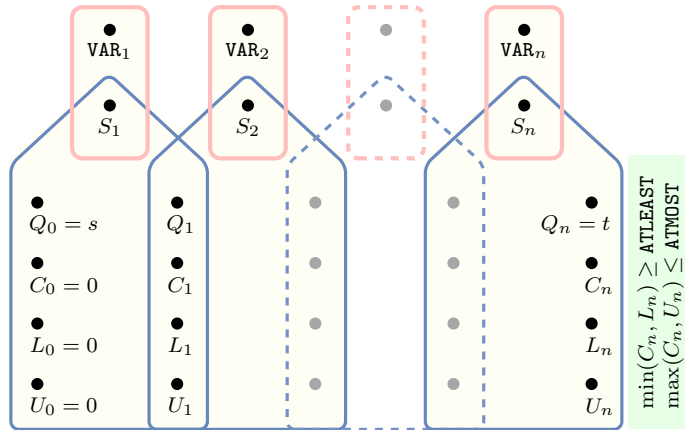


Figure 5.685: Hypergraph of the reformulation corresponding to the automaton of the `sliding_card_skip0` constraint