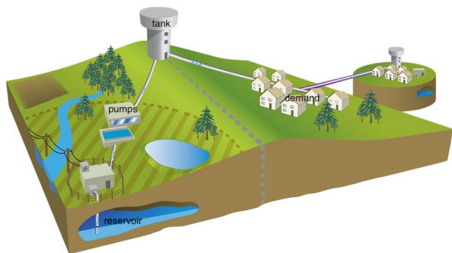
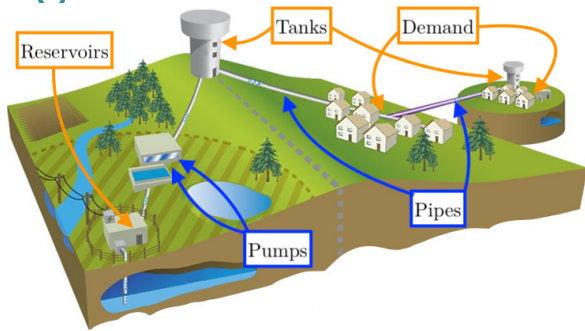


# Robust design of pumping stations in water distribution networks

Gratien Bonvin, Sophie Demassez, Wellington de Oliveira (CMA, Mines  
ParisTech/PSL)

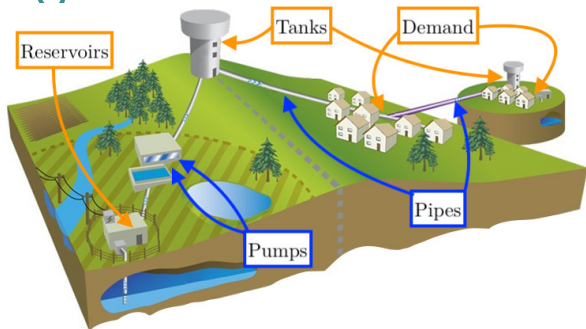


# drinking water distribution networks



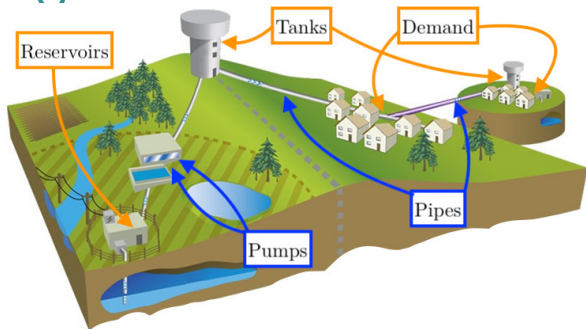
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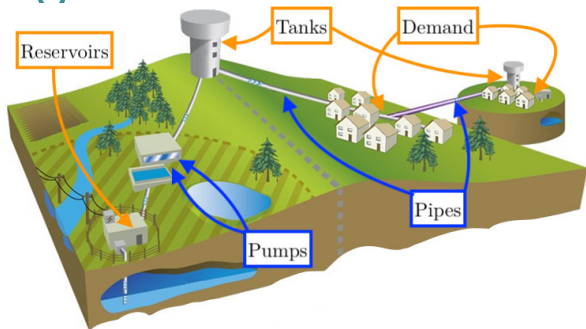
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- ▶ **pump scheduling**: given profiles of water demand and electricity tariff on a horizon  $T$  (resolution of 1h or 2h), decide when to switch on/off pumps  $K$  in order to satisfy the demand and the tank capacities at any time and to minimize energy costs

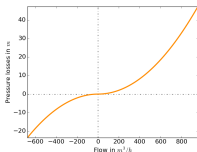
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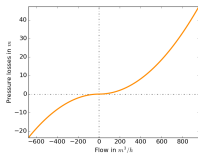
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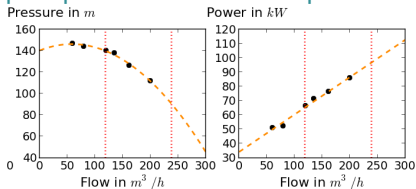
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## pump: head increase + power



$$\Delta h = -Gq^2 + H, \quad p = Cq + E$$

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# approximated pump scheduling

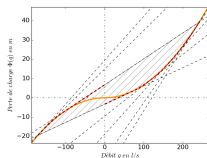
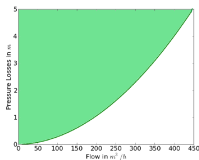
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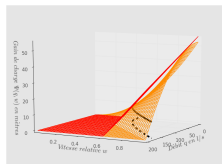
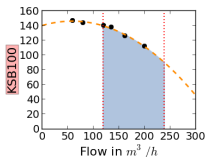
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  - ▶ **relax** the integrality and non-convex constraints: relax equalities or generate a tight polyhedral outer approximation (Bonvin19)
- pipes: one-direction / bi-direction



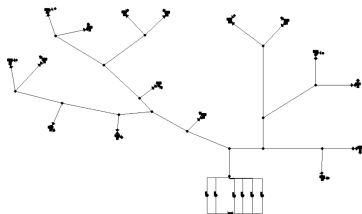
pumps: fixed-speed / variable-speed



# convex continuous relaxation

	Day	T=12			T=24			T=48		
		UB	LB	Gap	UB	LB	Gap	UB	LB	Gap
Simple FSD	21	inf	163.4	-	155.1	146.8	5.4%	150.9	145.9	3.3%
	22	inf	166.9	-	159.1	151.8	4.6%	155.7	150.2	3.5%
	23	inf	180.7	-	172.4	164.6	4.5%	168.5	162.8	3.4%
	24	inf	189.5	-	181.7	171.3	5.7%	176.0	170.3	3.2%
	25	inf	160.4	-	147.8	139.6	5.5%	145.5	139.7	4.0%
AT (M)	21	766.3	718.1	6.3%	733.2	719.0	1.9%	731.8	719.1	1.7%
	22	796.4	708.4	11.0%	732.1	708.5	3.2%	730.6	708.6	3.0%
	23	825.5	739.9	10.4%	761.5	740.6	2.7%	765.0	740.8	3.2%
	24	884.2	800.0	9.5%	822.9	800.8	2.7%	824.0	801.2	2.8%
	25	845.8	654.8	22.6%	690.6	656.3	5.0%	685.6	656.4	4.3%
Poormond	21	111.6	100.8	9.7%	109.0	99.6	8.6%	110.1	99.6	9.5%
	22	113.6	102.1	10.1%	113.0	101.1	10.5%	112.4	101.0	10.1%
	23	126.6	114.2	9.8%	125.2	112.9	9.8%	124.5	112.8	9.4%
	24	138.9	124.7	10.2%	136.3	123.2	9.6%	136.0	123.1	9.5%
	25	113.4	94.2	16.9%	94.2	85.2	9.6%	92.4	85.1	7.9%
Simple VSD	21	148.2	135.0	8.9%	146.8	117.8	19.8%	146.9	108.7	26.0%
	22	154.0	140.0	9.1%	152.4	122.8	19.4%	151.5	113.5	25.1%
	23	167.5	153.0	8.7%	165.1	134.9	18.3%	164.0	124.1	24.3%
	24	173.5	157.8	9.0%	172.2	138.1	19.8%	171.2	127.6	25.5%
	25	145.0	129.9	10.4%	139.8	111.2	20.5%	140.9	103.2	26.8%
DWG	21	3379.3	3263.0	3.4%	-	3228.1	-	-	3230.2	-
	22	3398.2	3274.1	3.7%	3420.6	3229.8	5.6%	-	3229.6	-
	23	3555.6	3419.6	3.8%	-	3376.4	-	-	3376.2	-
	24	3689.4	3458.7	3.8%	3737.5	3516.4	5.9%	-	3516.1	-
	25	3477.2	3122.2	10.2%	3312.7	3097.4	6.5%	3360.4	3097.4	7.8%
FRD	29.01				126.2	122.7	2.8%	127.5	122.7	3.8%
	27.03				138.4	132.5	4.3%	137.5	132.5	3.6%
	30.05				103.4	100.6	2.7%	103.9	100.6	3.2%
	26.07				216.4	200.6	7.3%	-	200.5	-
	28.09				105.9	100.5	5.1%	103.9	100.5	3.3%
24.11				104.4	101.1	3.2%	103.6	101.1	2.4%	

- ▶ lower bound computed after b&b presolve
- ▶ mean gap 9.5% to the best solution known
- ▶ for considered benchmark **FRD: 4%**



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**Proposition:** for branched networks as FRD, if  $Q_k^{\min} = 0$  for each pump class  $k$ , then the binary **pump operation variables can be aggregated** per pump class and **their integrality relaxed** for the classes of pumps able to exceed the highest allowed head increase.

# unfeasibility and dominance

- ▶ if a configuration with  $Y_k$  pumps in each class  $k$  is unfeasible then at least one more pump should be installed:  $\sum_k y_k Y_k \geq 1$  (feasibility cut) with  $y_{kn} = 1$  if at least  $n + 1$  pumps of class  $k$  are installed

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# Benders decomposition

1. initialize  $\mathcal{F} = \mathcal{F}_0, \mathcal{O} = \emptyset, UB = +\infty$
2. solve the master program, get  $y^*$  and  $LB = \sum_{k,n} I_k y_{kn}^* + z^*$

$$\begin{aligned} \min_{y \in \{0,1\}^{K\tilde{N}}, z \geq 0} \quad & \sum_{k,n} I_k y_{kn} + z \\ \text{s.t.} \quad & y_{kn} \geq y_{kn+1}, & \forall k, n \\ & z \geq c(Y) + s(Y)(y - Y), & \forall Y \in \mathcal{O} \\ & \sum_{k \in K} y_k Y_k \geq 1, & \forall Y \in \mathcal{F} \end{aligned}$$

3. check configuration  $y^*$  on the critical days, if unfeasible add to  $\mathcal{F}$  with all the identified dominated maximal configurations
4. otherwise, get the operation cost  $c(y^*)$  and a subgradient  $s(y^*)$  of  $c$  at  $y^*$  by solving the relaxed daily pump scheduling NLPs and add  $y^*$  to  $\mathcal{O}$ ; update  $UB = \min(UB, \sum_{k,n} I_k y_{kn}^* + c(y^*))$
5. stop if  $UB - LB \leq \epsilon$ , otherwise iterate

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- ▶ extension to the pump+pipe design ? generalization to wider classes of networks ?