5.34 assign_and_counts

	DESCRIPTION	LINKS	GRAPH	AUTOMATON
Origin	N. Beldiceanu			
Constraint	assign_and_counts(COLO	URS, ITEMS, RELOP, LI	IMIT)	
Arguments	COLOURS : collectic ITEMS : collectic RELOP : atom LIMIT : dvar	n(val-int) n(bin-dvar, colour	-dvar)	
Restrictions	$\begin{array}{c} \textbf{required}(\texttt{COLOURS},\texttt{val})\\ \textbf{distinct}(\texttt{COLOURS},\texttt{val})\\ \textbf{required}(\texttt{ITEMS},[\texttt{bin},\texttt{c}]\\ \texttt{RELOP} \in [=,\neq,<,\geq,>,\end{array}$) olour]) ≤]		
Purpose	Given several items (each fixed), and different bins, a of colour COLOURS in each	of them having a spective sign each item to a bi bin satisfies the condition	cific colour that may not	t be initially er n of items
	$(\langle 4 \rangle)$)	1	

colour - 4,

colour - 5

bin - 3 colour -4,

bin - 1 colour -4,

 $\mathtt{bin}-1$

 $\mathtt{bin}-1$

Example

Figure 5.80 shows the solution associated with the example. The items and the bins are respectively represented by little squares and by the different columns. Each little square contains the value of the key attribute of the item to which it corresponds. The items for which the colour attribute is equal to 4 are located under the thick line.

 $\leq, 2$



Figure 5.80: Assignment of the items to the bins

The assign_and_counts constraint holds since for each used bin (i.e., namely bins 1 and 3) the number of assigned items for which the colour attribute is equal to 4 is less than or equal to the limit 2.

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Typical	$\begin{split} \texttt{COLOURS} &> 0 \\ \texttt{ITEMS} &> 1 \\ \texttt{range}(\texttt{ITEMS.bin}) &> 1 \\ \texttt{RELOP} \in [<, \leq] \\ \texttt{LIMIT} &> 0 \\ \texttt{LIMIT} &< \texttt{ITEMS} \end{split}$		
Symmetries	• Items of COLOURS are permutable.		
	• Items of ITEMS are permutable.		
	• All occurrences of two distinct values of ITEMS.bin can be swapped; all occurrences of a value of ITEMS.bin can be renamed to any unused value.		
Arg properties			
ing. Properties	• Contractible wrt. ITEMS when $\text{RELOP} \in [<, \leq]$.		
	• Extensible wrt. ITEMS when $RELOP \in [\geq, >]$.		
Usage	Some persons have pointed out that it is impossible to use constraints such as among, atleast, atmost, count, or global_cardinality if the set of variables is not initially known. However, this is for instance required in practice for some timetabling problems.		
See also	assignment dimension removed: count, counts.		
	used in graph description: counts.		
Keywords	application area: assignment.		
	characteristic of a constraint: coloured, automaton, automaton with array of counters, derived collection.		
	final graph structure: acyclic, bipartite, no loop.		
	modelling: assignment dimension.		

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Derived Collection	<pre>col(VALUES-collection(val-int),[item(val-COLOURS.val)])</pre>		
Arc input(s)	ITEMS ITEMS		
Arc generator	$PRODUCT \mapsto \texttt{collection}(\texttt{items1},\texttt{items2})$		
Arc arity	2		
Arc constraint(s)	${\tt items1.bin} = {\tt items2.bin}$		
Graph class	ACYCLICBIPARTITENO_LOOP		
Sets	$ \left[\begin{array}{c} SUCC \mapsto \\ \left[\begin{array}{c} source, \\ variables - col \left(\begin{array}{c} VARIABLES - collection(var - dvar), \\ [\texttt{item}(var - ITEMS.colour)] \end{array} \right) \end{array} \right] $		
Constraint(s) on sets	<pre>counts(VALUES, variables, RELOP, LIMIT)</pre>		

We enforce the **counts** constraint on the colour of the items that are assigned to the same bin.

Parts (A) and (B) of Figure 5.81 respectively show the initial and final graph associated with the **Example** slot. The final graph consists of the following two connected components:

- The connected component containing six vertices corresponds to the items that are assigned to bin 1.
- The connected component containing two vertices corresponds to the items that are assigned to bin 3.



Figure 5.81: Initial and final graph of the assign_and_counts constraint

The assign_and_counts constraint holds since for each set of successors of the vertices of the final graph no more than two items take colour 4.

Graph model

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Automaton

Figure 5.82 depicts the automaton associated with the assign_and_courts constraint. To each colour attribute $COLOUR_i$ of the collection ITEMS corresponds a 0-1 signature variable S_i . The following signature constraint links $COLOUR_i$ and S_i : $COLOUR_i \in COLOURS \Leftrightarrow S_i$. For all items of the collection ITEMS for which the colour attribute takes its value in COLOURS, counts for each value assigned to the bin attribute its number of occurrences n, and finally imposes the condition n RELOP LIMIT.



Figure 5.82: Automaton of the assign_and_counts constraint