

5.51 big_peak

	DESCRIPTION	LINKS	AUTOMATON
Origin	Derived from peak .		
Constraint	<code>big_peak(N, VARIABLES, TOLERANCE)</code>		
Arguments	<code>N</code> : <code>dvar</code> <code>VARIABLES</code> : <code>collection(var-dvar)</code> <code>TOLERANCE</code> : <code>int</code>		
Restrictions	$N \geq 0$ $2 * N \leq \max(VARIABLES - 1, 0)$ <code>required(VARIABLES, var)</code> $TOLERANCE \geq 0$		
Purpose	<p>A variable V_p ($1 < p < m$) of the sequence of variables $VARIABLES = V_1, \dots, V_m$ is a <i>peak</i> if and only if there exists an i ($1 < i \leq p$) such that $V_{i-1} < V_i$ and $V_i = V_{i+1} = \dots = V_p$ and $V_p > V_{p+1}$. Similarly a variable V_v ($1 < k < m$) is a <i>valley</i> if and only if there exists an i ($1 < i \leq v$) such that $V_{i-1} > V_i$ and $V_i = V_{i+1} = \dots = V_v$ and $V_v < V_{v+1}$. A peak variable V_p ($1 < p < m$) is a <i>potential big peak</i> wrt a non-negative integer $TOLERANCE$ if and only if:</p> <ol style="list-style-type: none"> V_p is a peak, $\exists i, j \in [1, m] \mid i < p < j, V_i$ is a valley (or $i = 1$ if there is no valley before position p), V_j is a valley (or $i = m$ if there is no valley after position p), $V_p - V_i > TOLERANCE$, and $V_p - V_j > TOLERANCE$. <p>Let i_p and j_p be the largest i and the smallest j satisfying condition 2. Now a potential big peak V_p ($1 < p < m$) is a <i>big peak</i> if and only if the interval $[i, j]$ does not contain any potential big peak that is strictly higher than V_p. The constraint <code>big_peak</code> holds if and only if N is the total number of big peaks of the sequence of variables $VARIABLES$.</p>		
Example	<div style="border: 1px solid blue; padding: 5px;"> $(7, \langle 4, 2, 2, 4, 3, 8, 6, 7, 7, 9, 5, 6, 3, 12, 12, 6, 6, 8, 4, 5, 1 \rangle, 0)$ $(4, \langle 4, 2, 2, 4, 3, 8, 6, 7, 7, 9, 5, 6, 3, 12, 12, 6, 6, 8, 4, 5, 1 \rangle, 1)$ </div> <p>As shown part Part (A) of Figure 5.116, the first <code>big_peak</code> constraint holds since the sequence 4 2 2 4 3 8 6 7 7 9 5 6 3 12 12 6 6 8 4 5 1 contains seven big peaks wrt a tolerance of 0 (i.e., we consider standard peaks).</p> <p>As shown part Part (B) of Figure 5.116, the second <code>big_peak</code> constraint holds since the same sequence 4 2 2 4 3 8 6 7 7 9 5 6 3 12 12 6 6 8 4 5 1 contains only four big peaks wrt a tolerance of 1.</p>		
Typical	$N \geq 1$ $ VARIABLES > 6$ <code>range(VARIABLES.var) > 1</code> $TOLERANCE > 1$		

Symmetries

- Items of VARIABLES can be [reversed](#).
- One and the same constant can be [added](#) to the `var` attribute of all items of VARIABLES.

Arg. properties

- [Functional dependency](#): N determined by VARIABLES and TOLERANCE.
- [Contractible](#) wrt. VARIABLES when $N = 0$ and $TOLERANCE = 0$.

Usage

Useful for constraining the number of *big peaks* of a sequence of domain variables, by ignoring too small valleys that artificially create small peaks wrt TOLERANCE.

See also

[specialisation: peak](#) (*the tolerance is set to 0 and removed*).

Keywords

[characteristic of a constraint](#): automaton, automaton with counters.

[combinatorial object](#): sequence.

[constraint arguments](#): pure functional dependency.

[modelling](#): functional dependency.

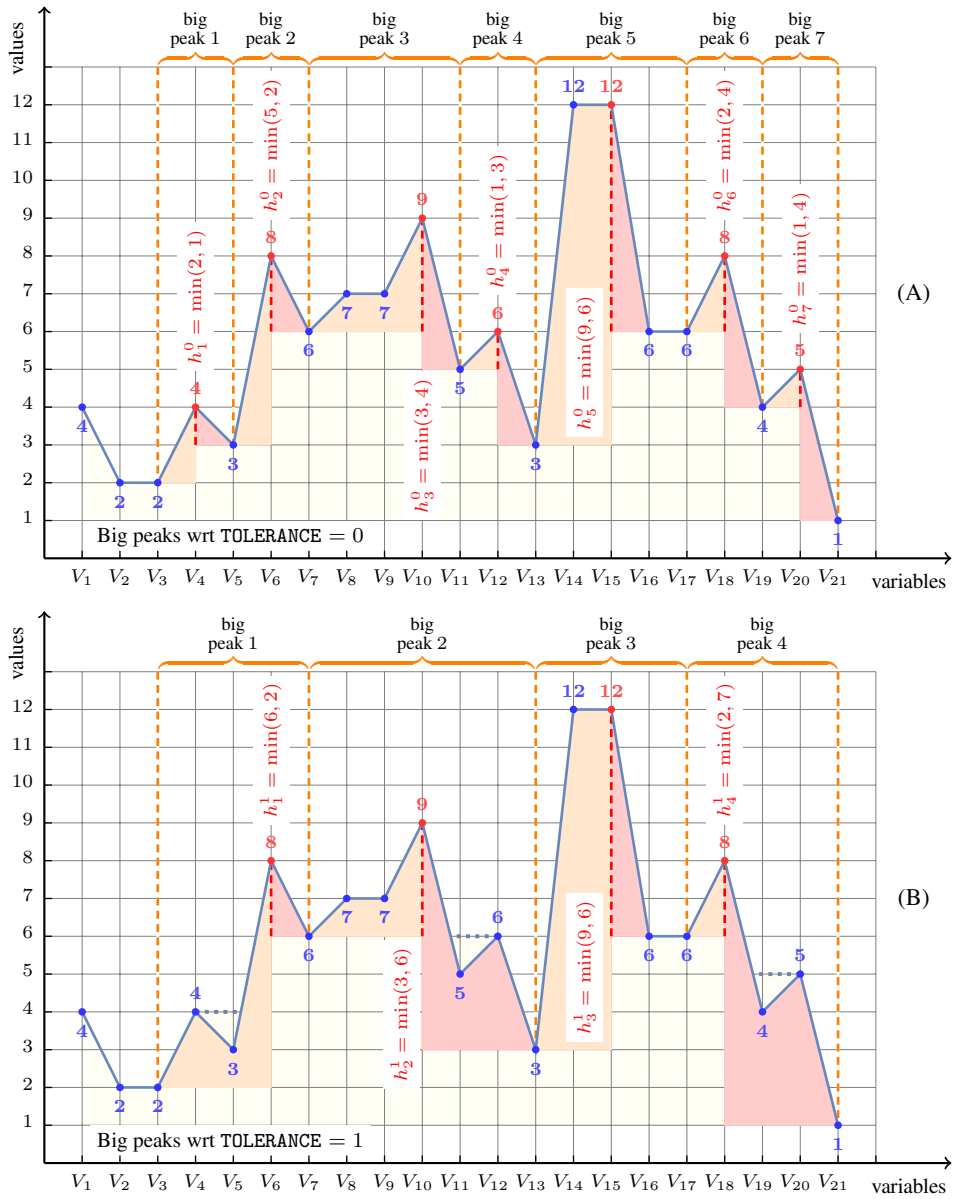


Figure 5.116: Illustration of the **Example** slot: Part (A) a sequence of 21 variables V_1, V_2, \dots, V_{21} respectively fixed to values 4, 2, 2, 4, 3, 8, 6, 7, 7, 9, 5, 6, 3, 12, 12, 6, 6, 8, 4, 5, 1 and its corresponding 7 peaks (TOLERANCE = 0 corresponds to standard peaks) with their respective heights $h_1^0 = 1, h_2^0 = 2, h_3^0 = 3, h_4^0 = 1, h_5^0 = 6, h_6^0 = 2, h_7^0 = 1$ (the left and right hand sides of each peak are coloured in light orange and light red) Part (B) the same sequence of variables and its 4 big peaks when TOLERANCE = 1 with their respective heights $h_1^1 = 2, h_2^1 = 3, h_3^1 = 6, h_4^1 = 2$

Automaton

Figure 5.117 depicts the automaton associated with the `big_peak` constraint. To each pair of consecutive variables ($\text{VAR}_i, \text{VAR}_{i+1}$) of the collection `VARIABLES` corresponds a signature variable S_i . The following signature constraint links $\text{VAR}_i, \text{VAR}_{i+1}$ and S_i : $(\text{VAR}_i < \text{VAR}_{i+1} \Leftrightarrow S_i = 0) \wedge (\text{VAR}_i = \text{VAR}_{i+1} \Leftrightarrow S_i = 1) \wedge (\text{VAR}_i > \text{VAR}_{i+1} \Leftrightarrow S_i = 2)$.

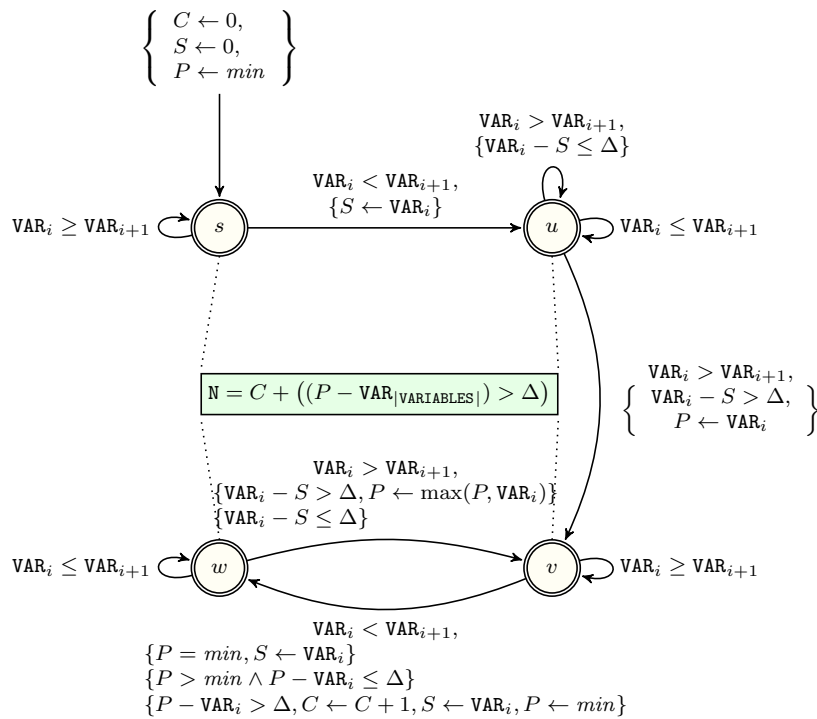


Figure 5.117: Automaton for the `big_peak` constraint where C , S , P , \min and Δ respectively stand for the number of big peaks already encountered, the altitude at the start of the current potential big peak, the altitude of the current potential big peak, the smallest value that can be assigned to a variable of `VARIABLES`, the TOLERANCE parameter