

## 5.111 decreasing\_peak

	DESCRIPTION	LINKS	AUTOMATON
<b>Origin</b>	Derived from <a href="#">peak</a> and <a href="#">decreasing</a> .		
<b>Constraint</b>	<code>decreasing_peak(VARIABLES)</code>		
<b>Argument</b>	VARIABLES : <code>collection(var-dvar)</code>		
<b>Restrictions</b>	$ VARIABLES  > 0$ <code>required(VARIABLES, var)</code>		
<b>Purpose</b>	<p>A variable <math>V_k</math> (<math>1 &lt; k &lt; m</math>) of the sequence of variables <math>VARIABLES = V_1, \dots, V_m</math> is a <i>peak</i> if and only if there exists an <math>i</math> (<math>1 &lt; i \leq k</math>) such that <math>V_{i-1} &lt; V_i</math> and <math>V_i = V_{i+1} = \dots = V_k</math> and <math>V_k &gt; V_{k+1}</math>.</p> <p>When considering all the peaks of the sequence <math>VARIABLES</math> from left to right enforce all peaks to be decreasing, i.e. the altitude of each peak is less than or equal to the altitude of its preceding peak when it exists.</p>		
<b>Example</b>	$((1, 7, 7, 4, 3, 7, 2, 2, 5, 4))$		

The `decreasing_peak` constraint holds since the sequence 1 7 7 4 3 7 2 2 5 4 contains three peaks, in bold, that are decreasing.

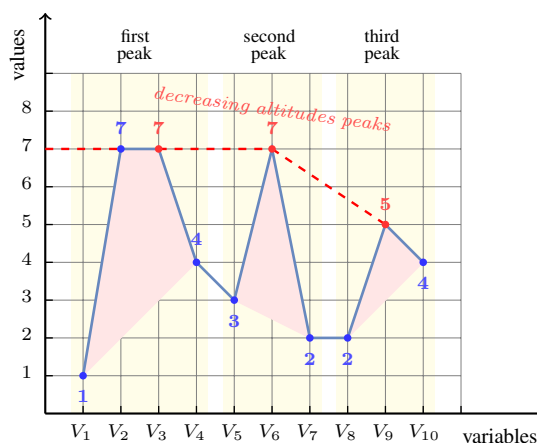


Figure 5.245: Illustration of the **Example** slot: a sequence of ten variables  $V_1, V_2, V_3, V_4, V_5, V_6, V_7, V_8, V_9, V_{10}$  respectively fixed to values 1, 7, 7, 4, 3, 7, 2, 2, 5, 4 and its corresponding three peaks, in red, respectively located at altitudes 7, 7 and 5

**Typical**

```

|VARIABLES| ≥ 7
range(VARIABLES.var) > 1
peak(VARIABLES.var) ≥ 3

```

**Symmetry**

One and the same constant can be [added](#) to the var attribute of all items of VARIABLES.

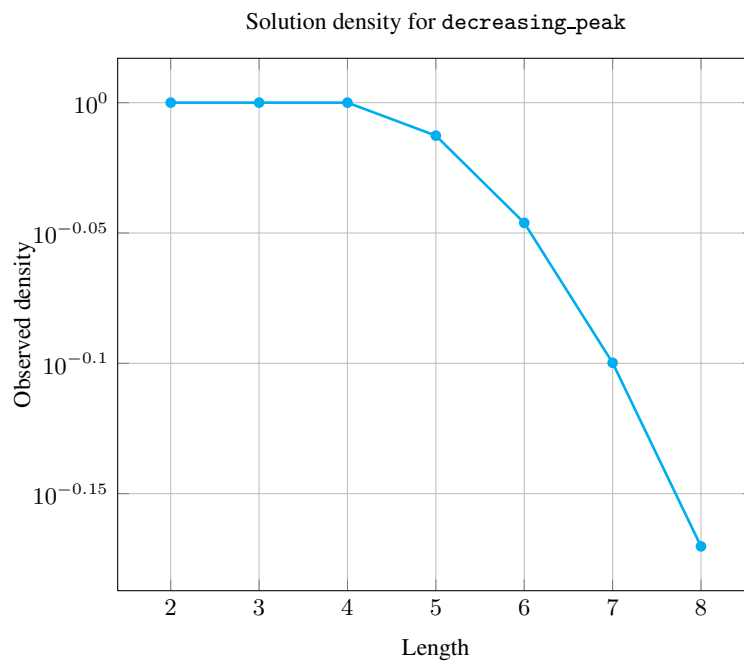
**Arg. properties**

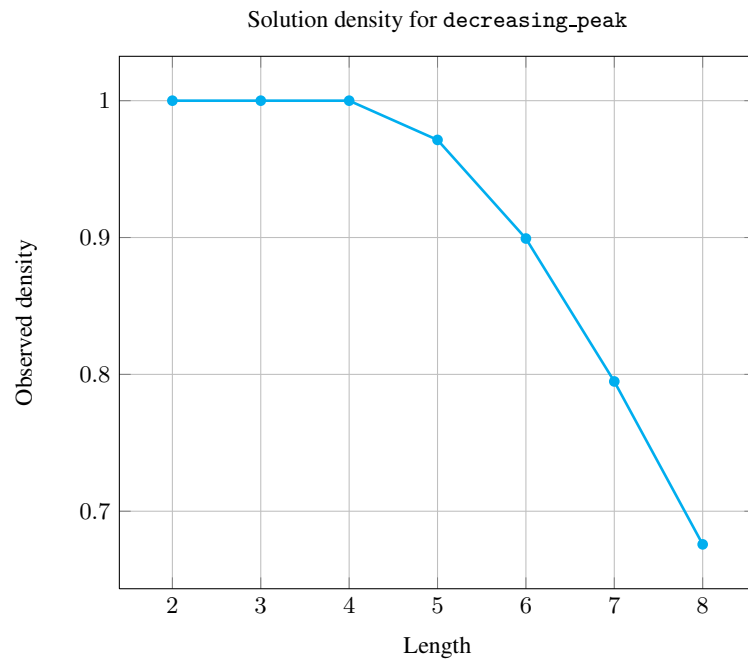
- [Prefix-contractible](#) wrt. VARIABLES.
- [Suffix-contractible](#) wrt. VARIABLES.

**Counting**

Length ( $n$ )	2	3	4	5	6	7	8
Solutions	9	64	625	7553	105798	1666878	29090469

Number of solutions for `decreasing_peak`: domains  $0..n$



**See also**

**implied by:** [all\\_equal\\_peak](#).

**related:** [increasing\\_peak](#), [peak](#).

**Keywords**

**characteristic of a constraint:** [automaton](#), [automaton with counters](#),  
[automaton with same input symbol](#).

**combinatorial object:** [sequence](#).

**constraint network structure:** [sliding cyclic\(1\) constraint network\(2\)](#).

**Cond. implications**

`decreasing_peak(VARIABLES)`  
 with `peak(VARIABLES.var) > 0`  
**implies** `not_all_equal(VARIABLES)`.

**Automaton**

Figure 5.246 depicts the automaton associated with the `decreasing_peak` constraint. To each pair of consecutive variables  $(VAR_i, VAR_{i+1})$  of the collection `VARIABLES` corresponds a signature variable  $S_i$ . The following signature constraint links  $VAR_i, VAR_{i+1}$  and  $S_i$ :  $(VAR_i < VAR_{i+1} \Leftrightarrow S_i = 0) \wedge (VAR_i = VAR_{i+1} \Leftrightarrow S_i = 1) \wedge (VAR_i > VAR_{i+1} \Leftrightarrow S_i = 2)$ .

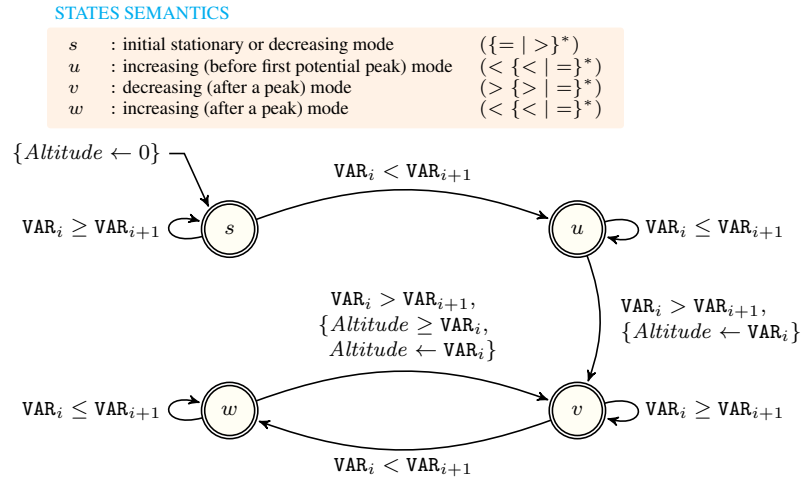


Figure 5.246: Automaton for the `decreasing_peak` constraint (note the conditional transition from state  $w$  to state  $v$  testing that the counter  $Altitude$  is greater than or equal to  $VAR_i$  for enforcing that all peaks from left to right are in decreasing altitude)

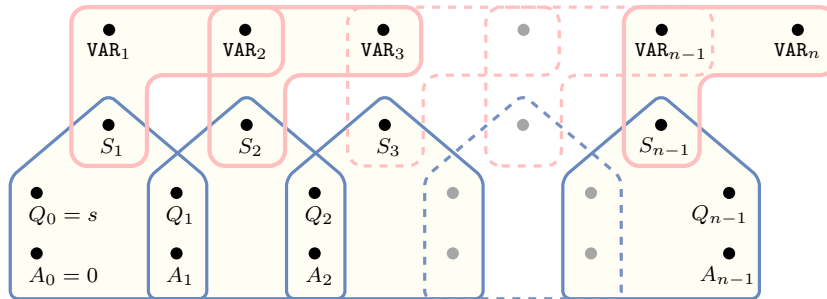


Figure 5.247: Hypergraph of the reformulation corresponding to the automaton of the `decreasing_peak` constraint where  $A_i$  stands for the value of the counter  $Altitude$  (since all states of the automaton are accepting there is no restriction on the last variable  $Q_{n-1}$ )