

## 5.119 diffn\_column

	DESCRIPTION	LINKS	GRAPH
<b>Origin</b>	CHIP: option guillotine cut (column) of <code>diffn</code> .		
<b>Constraint</b>	<code>diffn_column(ORTHOTOPES, DIM)</code>		
<b>Type</b>	ORTHOTOPE : <code>collection(ori-dvar, siz-dvar, end-dvar)</code>		
<b>Arguments</b>	ORTHOTOPES : <code>collection(orth - ORTHOTOPE)</code> DIM : <code>int</code>		
<b>Restrictions</b>	<code> ORTHOTOPE  &gt; 0</code> <code>require_at_least(2, ORTHOTOPE, [ori, siz, end])</code> <code>ORTHOTOPE.siz ≥ 0</code> <code>ORTHOTOPE.ori ≤ ORTHOTOPE.end</code> <code>required(ORTHOTOPES, orth)</code> <code>same_size(ORTHOTOPES, orth)</code> <code>DIM &gt; 0</code> <code>DIM ≤  ORTHOTOPE </code> <code>diffn(ORTHOTOPES)</code>		

Extension of the generalised multi-dimensional non-overlapping `diffn` constraint. Holds if, for each pair of `orthotopes` ( $O_1, O_2$ ) the following conditions hold:

### Purpose

- $O_1$  and  $O_2$  do not overlap. Two `orthotopes` do not overlap if one of the orthotopes has zero size or if there exists at least one dimension where their projections do not overlap.
- Let  $P_1$  and  $P_2$  respectively denote the projections of  $O_1$  and  $O_2$  onto dimension DIM. If  $P_1$  and  $P_2$  overlap then the size of their intersection is equal to the size of  $O_1$  in dimension DIM, as well as to the size of  $O_2$  in dimension DIM.

### Example

$$\left( \begin{array}{l} \text{orth} - \langle \mathbf{ori} - 1 \ \mathbf{siz} - 3 \ \mathbf{end} - 4, \mathbf{ori} - 3 \ \mathbf{siz} - 2 \ \mathbf{end} - 5 \rangle, \\ \text{orth} - \langle \mathbf{ori} - 9 \ \mathbf{siz} - 1 \ \mathbf{end} - 10, \\ \mathbf{ori} - 4 \ \mathbf{siz} - 3 \ \mathbf{end} - 7 \rangle, \\ \text{orth} - \langle \mathbf{ori} - 4 \ \mathbf{siz} - 2 \ \mathbf{end} - 6, \mathbf{ori} - 3 \ \mathbf{siz} - 4 \ \mathbf{end} - 7 \rangle, \\ \text{orth} - \langle \mathbf{ori} - 1 \ \mathbf{siz} - 3 \ \mathbf{end} - 4, \mathbf{ori} - 6 \ \mathbf{siz} - 1 \ \mathbf{end} - 7 \rangle, \\ \text{orth} - \langle \mathbf{ori} - 6 \ \mathbf{siz} - 2 \ \mathbf{end} - 8, \mathbf{ori} - 1 \ \mathbf{siz} - 4 \ \mathbf{end} - 5 \rangle, \\ \text{orth} - \langle \mathbf{ori} - 10 \ \mathbf{siz} - 1 \ \mathbf{end} - 11, \\ \mathbf{ori} - 1 \ \mathbf{siz} - 1 \ \mathbf{end} - 2 \rangle, \\ \text{orth} - \langle \mathbf{ori} - 9 \ \mathbf{siz} - 1 \ \mathbf{end} - 10, \\ \mathbf{ori} - 1 \ \mathbf{siz} - 1 \ \mathbf{end} - 2 \rangle, \\ \text{orth} - \langle \mathbf{ori} - 6 \ \mathbf{siz} - 2 \ \mathbf{end} - 8, \mathbf{ori} - 6 \ \mathbf{siz} - 1 \ \mathbf{end} - 7 \rangle \end{array} \right), 1$$

Figure 5.268 represents the respective position of the eight rectangles of the example. The coordinates of the leftmost lowest corner of each rectangle are stressed in bold.

The `diffn_column` constraint holds since (1) the eight rectangles do not overlap and since (2) when their projection onto dimension DIM = 1 overlap the size of their intersection is equal to the size of the corresponding rectangles in dimension DIM = 1.

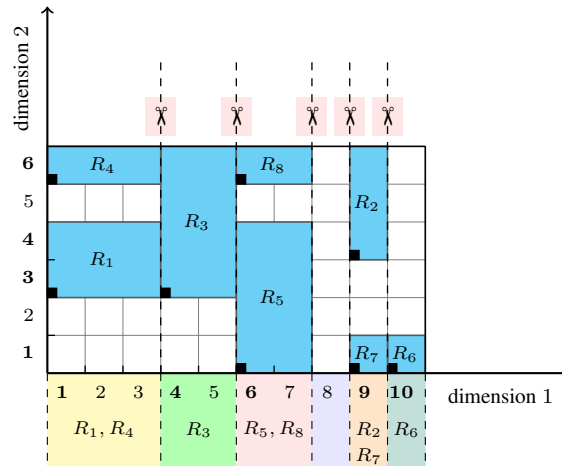


Figure 5.268: Illustration of the **Example** slot: eight non-overlapping rectangles such that, for each pair of rectangles  $R_i, R_j$  ( $1 \leq i < j \leq 8$ ), if the projections onto dimension 1 of rectangles  $R_i$  and  $R_j$  intersect then the size of their intersection is equal to the size of  $R_i$  in dimension 1 and to the size of  $R_j$  in dimension 1 (i.e. complete vertical strips along the border of any rectangle can be cut without crossing any rectangle)

#### Typical

```
|ORTHOTOPE| > 1
ORTHOTOPE.siz > 0
|ORTHOTOPES| > 1
```

#### Symmetries

- Items of ORTHOTOPES are [permutable](#).
- One and the same constant can be [added](#) to the `ori` and `end` attributes of all items of ORTHOTOPES.`orth`.

#### Arg. properties

[Contractible](#) wrt. ORTHOTOPES.

#### See also

**common keyword:** [diffn](#) (*geometrical constraint, orthotope*), [diffn\\_include](#) (*geometrical constraint, orthotope, positioning constraint*).

**implies:** [diffn\\_include](#).

**used in graph description:** [two\\_orth\\_column](#).

#### Keywords

**constraint type:** [decomposition](#).

**geometry:** [geometrical constraint](#), [positioning constraint](#), [orthotope](#), [guillotine cut](#).

<b>Arc input(s)</b>	ORTHOTOPES
<b>Arc generator</b>	$\text{CLIQUE}(<) \mapsto \text{collection}(\text{orthotopes1}, \text{orthotopes2})$
<b>Arc arity</b>	2
<b>Arc constraint(s)</b>	$\text{two\_orth\_column}(\text{orthotopes1.orth}, \text{orthotopes2.orth}, \text{DIM})$
<b>Graph property(ies)</b>	$\text{NARC} =  \text{ORTHOTOPES}  * ( \text{ORTHOTOPES}  - 1) / 2$

**Graph model**

Since showing all items produces too big graphs, parts (A) and (B) of Figure 5.269 respectively show the initial and final graph associated with the first three items of the **Example** slot. Since we use the **NARC** graph property, the arcs of the final graph are stressed in bold.

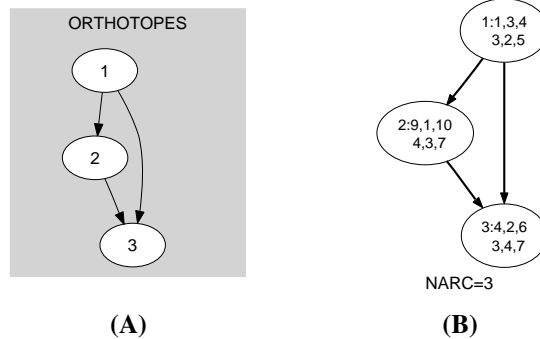


Figure 5.269: Initial and final graph of the diffn\_column constraint

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