

5.144 `element_sparse`

	DESCRIPTION	LINKS	GRAPH	AUTOMATON
Origin	CHIP			
Constraint	<code>element_sparse</code> (ITEM, TABLE, DEFAULT)			
Usual name	element			
Arguments	ITEM : <code>collection</code> (index-dvar, value-dvar) TABLE : <code>collection</code> (index-int, value-int) DEFAULT : <code>int</code>			
Restrictions	<code>required</code> (ITEM, [index, value]) ITEM.index ≥ 1 ITEM = 1 TABLE > 0 <code>required</code> (TABLE, [index, value]) TABLE.index ≥ 1 <code>distinct</code> (TABLE, index)			
Purpose	ITEM[1].value is equal to one of the entries of the table TABLE or to the default value DEFAULT if the entry ITEM[1].index does not exist in TABLE.			
Example	$\left(\left\langle \begin{array}{l} \langle \text{index} - 2 \text{ value} - 5 \rangle, \\ \text{index} - 1 \quad \text{value} - 6, \\ \langle \text{index} - 2 \text{ value} - 5, \\ \text{index} - 4 \text{ value} - 2, \\ \text{index} - 8 \text{ value} - 9 \end{array} \right\rangle, 5 \right)$			
	The <code>element_sparse</code> constraint holds since its first argument ITEM corresponds to the second item of the TABLE collection.			
Typical	TABLE > 1 <code>range</code> (TABLE.value) > 1			
Symmetries	<ul style="list-style-type: none"> Items of TABLE are <code>permutable</code>. All occurrences of two distinct values in ITEM.value, TABLE.value or DEFAULT can be <code>swapped</code>; all occurrences of a value in ITEM.value, TABLE.value or DEFAULT can be <code>renamed</code> to any unused value. 			
Usage	A sometimes more compact form of the <code>element</code> constraint: we are not obliged to specify explicitly the table entries that correspond to the specified default value. This can sometimes reduce drastically memory utilisation.			
Remark	The original constraint of <code>CHIP</code> had an additional parameter SIZE giving the maximum value of ITEM.index.			

Reformulation

Let I and V respectively denote $ITEM[1].index$ and $ITEM[1].value$. The `element_sparse`($ITEM, TABLE, DEFAULT$) constraint can be expressed in term of a reified constraint of the form:

$$\begin{aligned} & ((I = TABLE[1].index \wedge V = TABLE[1].value) \vee \\ & (I = TABLE[2].index \wedge V = TABLE[2].value) \vee \\ & \dots \\ & (I = TABLE[|TABLE|].index \wedge V = TABLE[|TABLE|].value)) \vee \\ & ((I \neq TABLE[1].index) \wedge \\ & (I \neq TABLE[2].index) \wedge \\ & \dots \\ & (I \neq TABLE[|TABLE|].index) \wedge \\ & (V = DEFAULT)). \end{aligned}$$
See also

common keyword: `elem`, `element` (*array constraint*), `elements_sparse` (*sparse table*).

implies: `elements_sparse`.

system of constraints: `elements_sparse`.

Keywords

characteristic of a constraint: `automaton`, `automaton without counters`, `reified automaton constraint`, `derived collection`.

constraint arguments: `binary constraint`.

constraint network structure: `centered cyclic(2) constraint network(1)`.

constraint type: `data constraint`.

filtering: `arc-consistency`.

modelling: `array constraint`, `table`, `sparse table`, `sparse functional dependency`, `variable indexing`.

Derived Collections

$$\text{col} \left(\begin{array}{l} \text{DEF-collection}(\text{index-int}, \text{value-int}), \\ [\text{item}(\text{index} - 0, \text{value} - \text{DEFAULT})] \end{array} \right)$$

$$\text{col} \left(\begin{array}{l} \text{TABLE_DEF-collection}(\text{index-dvar}, \text{value-dvar}), \\ [\text{item}(\text{index} - \text{TABLE.index}, \text{value} - \text{TABLE.value}), \\ \text{item}(\text{index} - \text{DEF.index}, \text{value} - \text{DEF.value})] \end{array} \right)$$
Arc input(s)

ITEM TABLE_DEF

Arc generator*PRODUCT* \mapsto *collection*(item, table_def)**Arc arity**

2

Arc constraint(s)

- item.value = table_def.value
- item.index = table_def.index \vee table_def.index = 0

Graph property(ies) $\overline{\text{NARC}} \geq 1$ **Graph model**

The final graph has between one and two arc constraints: it has two arcs when the default value DEFAULT occurs also in the table TABLE; otherwise it has only one arc.

Parts (A) and (B) of Figure 5.315 respectively show the initial and final graph associated with the **Example** slot. Since we use the $\overline{\text{NARC}}$ graph property the arcs of the final graph are outline with thick lines.

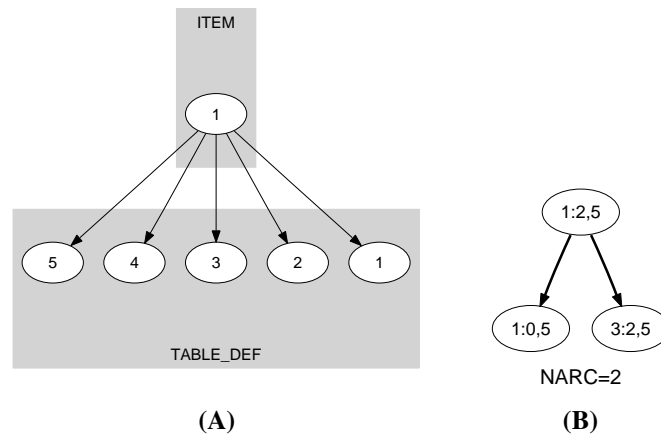


Figure 5.315: Initial and final graph of the *element_sparse* constraint

Automaton

Figure 5.316 depicts the automaton associated with the `element_sparse` constraint. Let `INDEX` and `VALUE` respectively be the index and the value attributes of the unique item of the `ITEM` collection. Let `INDEXi` and `VALUEi` respectively be the index and the value attributes of the *i*th item of the `TABLE` collection. To each quintuple $(INDEX, VALUE, DEFAULT, INDEX_i, VALUE_i)$ corresponds a signature variable S_i as well as the following signature constraint:

$$\left\{ \begin{array}{l} (INDEX \neq INDEX_i \wedge VALUE \neq DEFAULT) \Leftrightarrow S_i = 0 \wedge \\ (INDEX = INDEX_i \wedge VALUE = VALUE_i) \Leftrightarrow S_i = 1 \wedge . \\ (INDEX \neq INDEX_i \wedge VALUE = DEFAULT) \Leftrightarrow S_i = 2 \end{array} \right.$$

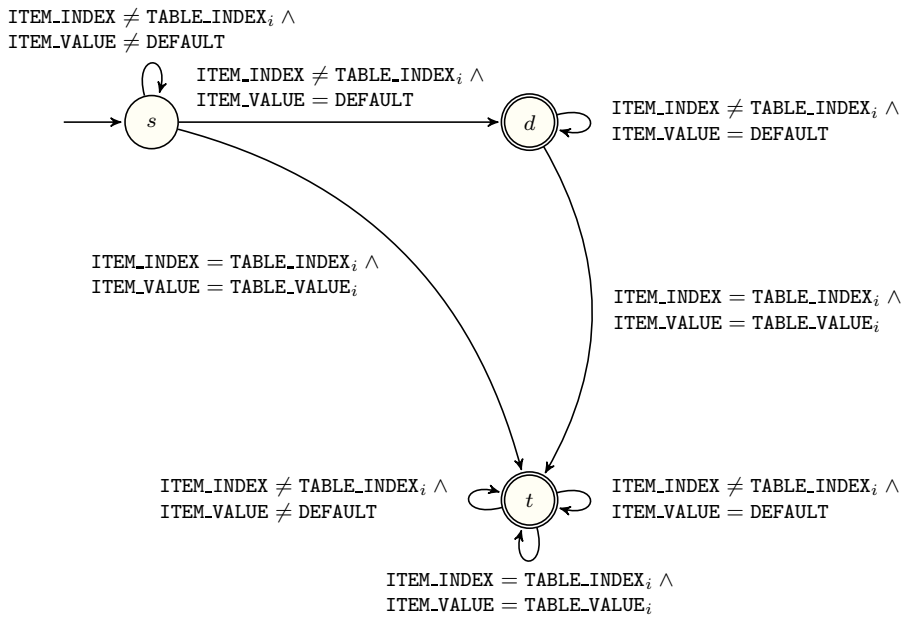


Figure 5.316: Automaton of the `element_sparse` constraint

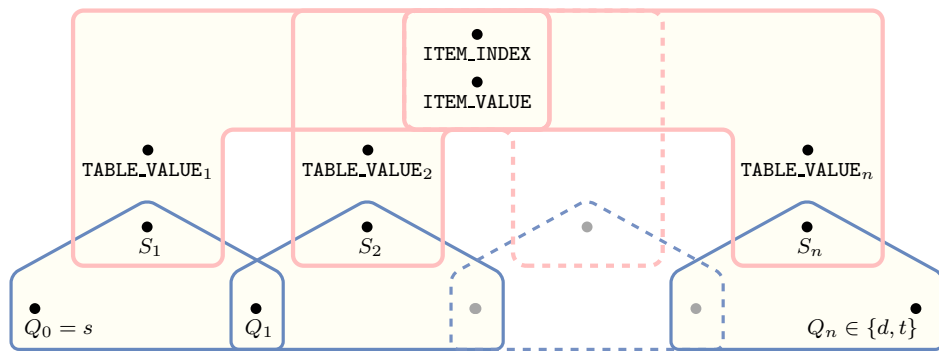


Figure 5.317: Hypergraph of the reformulation corresponding to the automaton of the `element_sparse` constraint

20030820

1163