

5.234 link_set_to_booleans

	DESCRIPTION	LINKS	GRAPH
Origin	Inspired by domain_constraint .		
Constraint	<code>link_set_to_booleans(SVAR, BOOLEANS)</code>		
Arguments	SVAR : <code>svar</code> BOOLEANS : <code>collection(bool-dvar, val-int)</code>		
Restrictions	<code>required(BOOLEANS, [bool, val])</code> <code>BOOLEANS.bool ≥ 0</code> <code>BOOLEANS.bool ≤ 1</code> <code>distinct(BOOLEANS, val)</code>		
Purpose	<div style="border: 1px solid pink; padding: 5px;"> Make the link between a set variable <i>SVAR</i> and those 0-1 variables that are associated with each potential value belonging to <i>SVAR</i>: The 0-1 variables, which are associated with a value belonging to the set variable <i>SVAR</i>, are equal to 1, while the remaining 0-1 variables are all equal to 0. </div>		
Example	<div style="border: 1px solid blue; padding: 10px; display: inline-block;"> $\left(\begin{array}{l} \{1, 3, 4\}, \\ \begin{array}{ll} \text{bool} - 0 & \text{val} - 0, \\ \text{bool} - 1 & \text{val} - 1, \\ \text{bool} - 0 & \text{val} - 2, \\ \text{bool} - 1 & \text{val} - 3, \\ \text{bool} - 1 & \text{val} - 4, \\ \text{bool} - 0 & \text{val} - 5 \end{array} \end{array} \right)$ </div> <p>In the example, the 0-1 variables associated with the values 1, 3 and 4 are all set to 1, while the other 0-1 variables are set to 0. Consequently, the <code>link_set_to_booleans</code> constraint holds since its first argument <i>SVAR</i> is set to $\{1, 3, 4\}$.</p>		
Typical	<code> BOOLEANS > 1</code> <code>range(BOOLEANS.bool) > 1</code>		
Symmetry	Items of <code>BOOLEANS</code> are permutable .		
Usage	This constraint is used in order to make the link between a formulation using set variables and a formulation based on linear programming.		
Systems	<code>channel</code> in Gecode , <code>link_set_to_booleans</code> in MiniZinc .		
See also	common keyword: alldifferent_between_sets , clique (<i>constraint involving set variables</i>), domain_constraint (<i>channelling constraint</i>), k_cut , path_from_to , roots , strongly_connected , symmetric_cardinality , symmetric_gcc , tour (<i>constraint involving set variables</i>).		

Keywords

characteristic of a constraint: derived collection.

constraint arguments: constraint involving set variables.

constraint type: decomposition, value constraint.

filtering: linear programming.

modelling: channelling constraint, set channel.

Derived Collection

$$\text{col} \left(\begin{array}{l} \text{SET-collection}(\text{one-int}, \text{setvar-svar}), \\ \text{item}(\text{one} - 1, \text{setvar} - \text{SVAR}) \end{array} \right)$$
Arc input(s)

SET BOOLEANS

Arc generator*PRODUCT* \mapsto collection(set, booleans)**Arc arity**

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Arc constraint(s)booleans.bool = set.one \Leftrightarrow in.set(booleans.val, set.setvar)**Graph property(ies)**NARC = |BOOLEANS|**Graph model**

The `link_set_to_booleans` constraint is modelled with the following bipartite graph. The first set of vertices corresponds to a single vertex containing the set variable. The second class of vertices contains one vertex for each item of the collection BOOLEANS. The arc constraint between the set variable SVAR and one potential value v of the set variable expresses the following:

- If the 0-1 variable associated with v is equal to 1 then v should belong to SVAR.
- Otherwise if the 0-1 variable associated with v is equal to 0 then v should not belong to SVAR.

Since all arc constraints should hold the final graph contains exactly |BOOLEANS| arcs.

Parts (A) and (B) of Figure 5.500 respectively show the initial and final graph associated with the **Example** slot. Since we use the **NARC** graph property, the arcs of the final graph are stressed in bold. The `link_set_to_booleans` constraint holds since the final graph contains exactly 6 arcs (one for each 0-1 variable).

Signature

Since the initial graph contains |BOOLEANS| arcs the maximum number of arcs of the final graph is equal to |BOOLEANS|. Therefore we can rewrite the graph property **NARC** = |BOOLEANS| to **NARC** \geq |BOOLEANS| and simplify NARC to **NARC**.

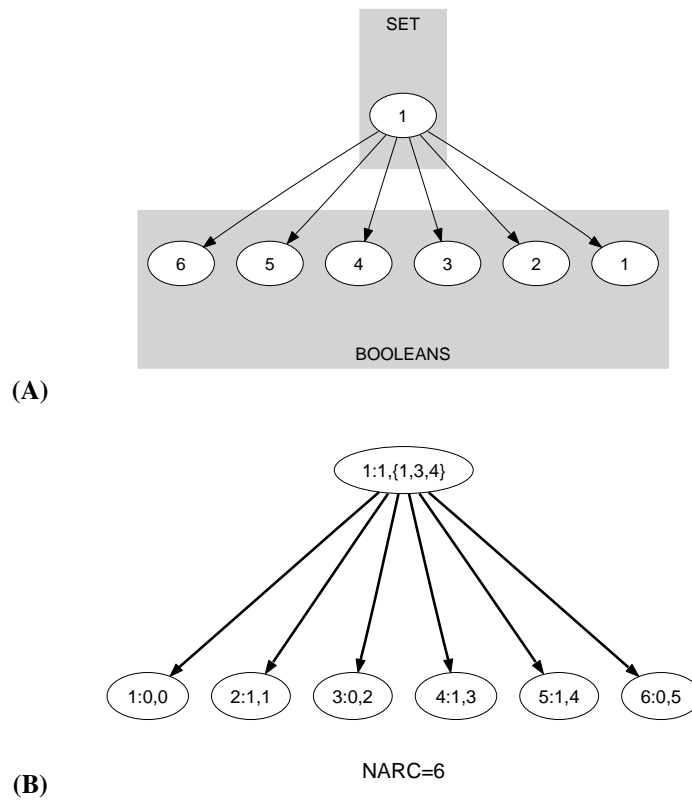


Figure 5.500: Initial and final graph of the link_set_to_booleans constraint